

# Numerical simulation of pressure oscillations in Francis turbine runners

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# Summary

1. Motivation
2. Problem and machine description
3. General numerical set-up
4. Parameters for the transient simulation
5. Results at the rated operating condition
6. Results at part load
7. Vortex shedding effects
8. Conclusions

## Motivation – General

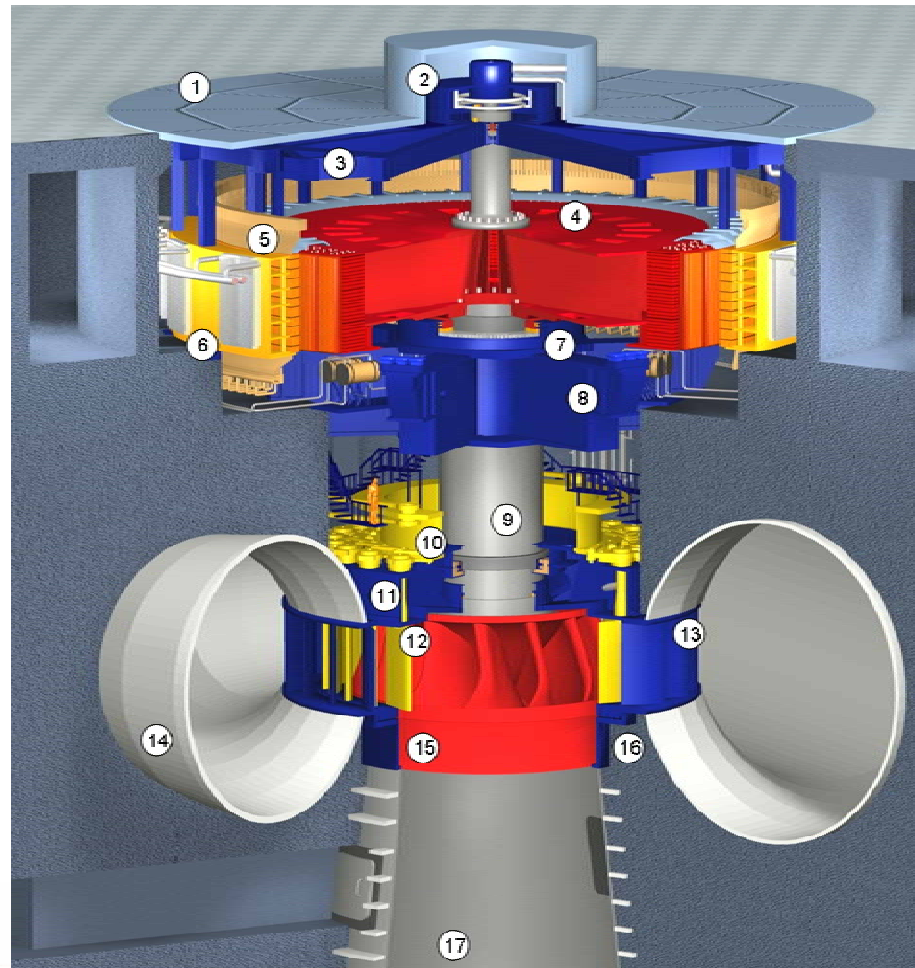
- Risk of runner cracks, causing energy generation loss, contractual penalties and repair costs.
  - Example:
    - $P = 200 \text{ MW} \times 3 \text{ Units}$ , Load Factor: 0,70
    - 3 Units down, each for 1 month, due to runner failures
    - Lost energy:  $\sim 18 \text{ Mio } \text{€}$
    - Contractual penalties:  $\sim 11 \text{ Mio } \text{€}$
    - Repair costs:  $\sim 0,8 \text{ Mio } \text{€}$  (New runner:  $\sim 2,0 \text{ Mio } \text{€}/\text{Runner}$ )
- Time and costs involved in a complete model test of a totally new hydraulic design

## Motivation – Technical

- Numerical prediction of pressure oscillations in hydraulic turbines, specially in Francis runners:
  - Rotor-stator interactions (RSI)
  - Draft tube instabilities (DTI)
  - Vortex shedding effects (VSE)
- Investigation and need of adequate turbulence models for the transient flow simulation
- CFD results as input for:
  - Accurate computational structural analysis (CSA)
  - Runner fatigue strength and fatigue life estimation

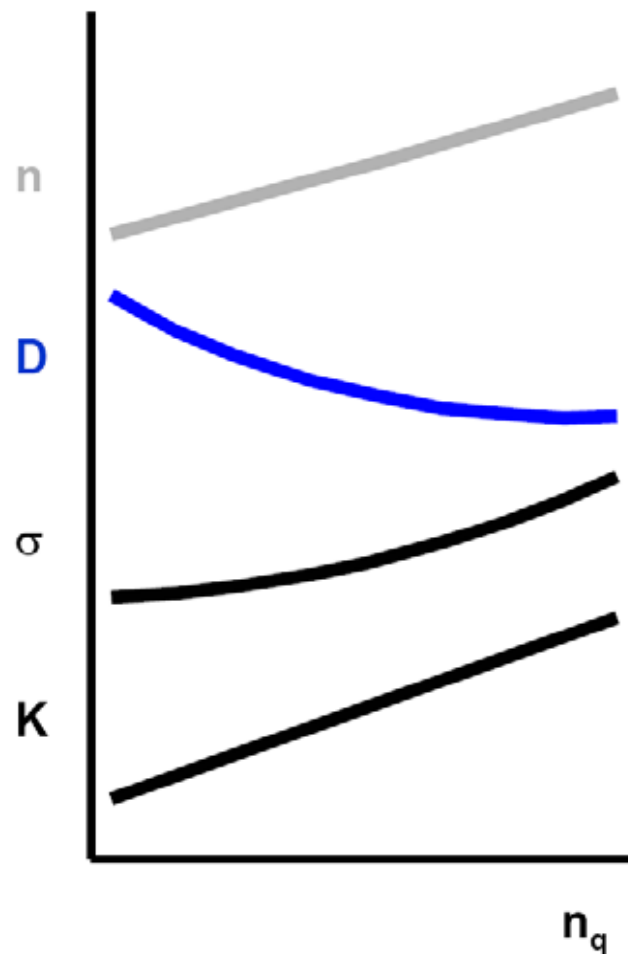


# Problem description – Definitions



- (1) Generator cover
- (2) Slip ring
- (3) Upper bracket
- (4) Generator rotor
- (5) Estator
- (6) Cooling
- (7) Brake
- (8) Lower bracket
- (9) Shaft
- (10) Operating ring
- (11) Head cover
- (12) Guide vanes
- (13) Stay vanes
- (14) Spiral case
- (15) Turbine runner
- (16) Bottom ring
- (17) Draft tube

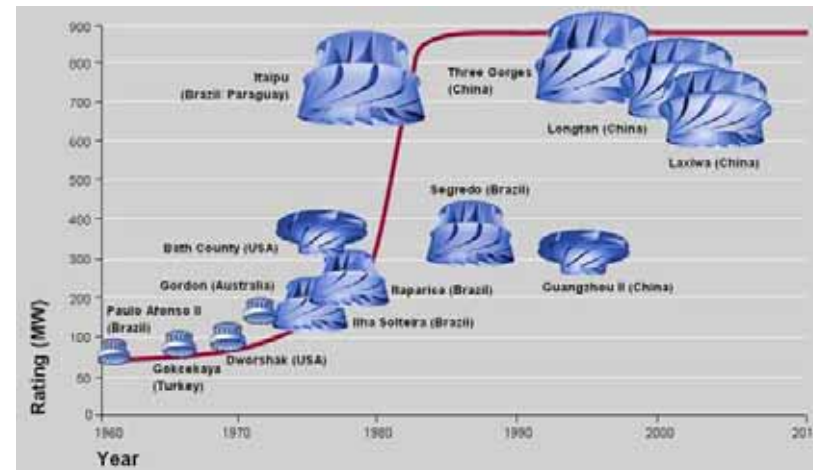
## Problem description – Structural loading



Higher specific speed  
 $(n_q = n\sqrt{Q}/H^{3/4})$  results in:

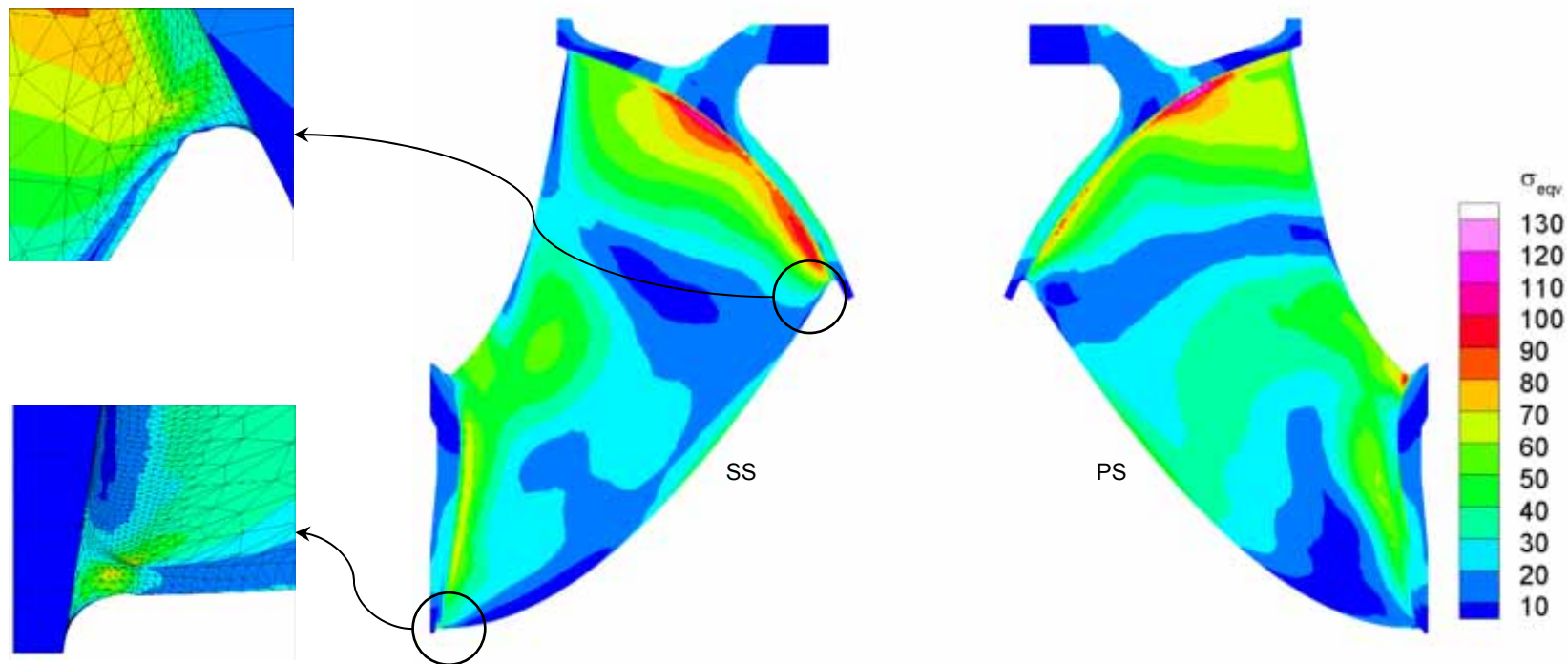
- Higher synchronous speed ( $n$ )  
 $\Rightarrow$  Lower generator cost
- Smaller size ( $D_{1a}$ ) of turbine runner  $\Rightarrow$  Lower turbine cost
- Higher cavitation factor ( $\sigma$ )  $\Rightarrow$  Higher suction head ( $h_s$ ) and increase in civil costs
- Increased “specific loading” ( $K = n_q\sqrt{H}$ ) of the hydraulic machine  $\Rightarrow$  **Increased loads over the turbine structure!**

# Problem description – Structural loading



- Increase of the specific load (K) over the years:
- Specific load of Three Gorges (2003, 1<sup>st</sup> Unit) about 10% higher than Itaipu (1984, 1<sup>st</sup> Unit).
- About 40% increase in the specific load over the last 50 years.

# Problem description – Structural problems



Example of equivalent von Mises structural static stresses

# Problem description – Structural problems

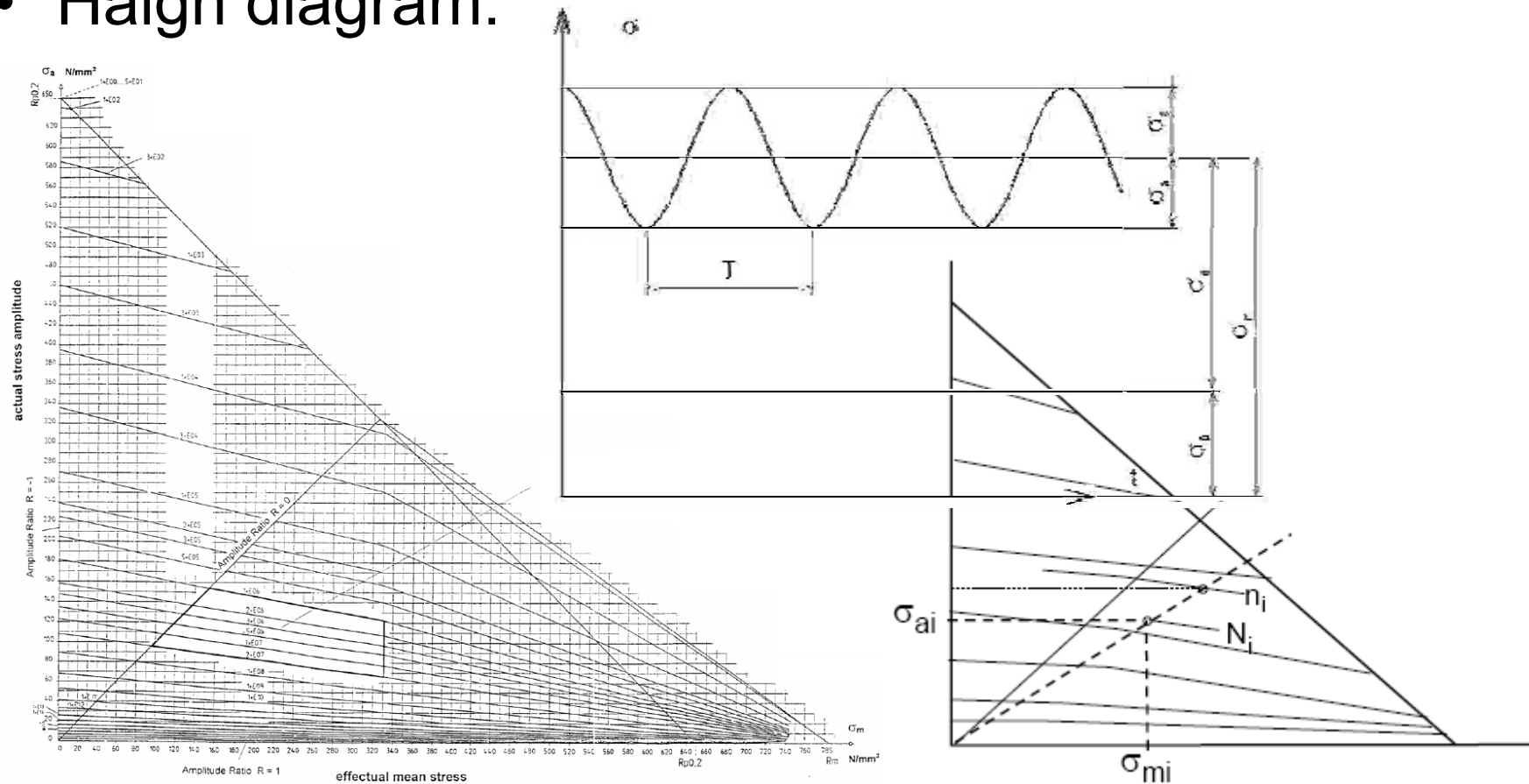


Runner cracks at the trailing edge at the crown and band



# Problem description – Fatigue analysis

- Haigh diagram:



# Problem description – Measuring

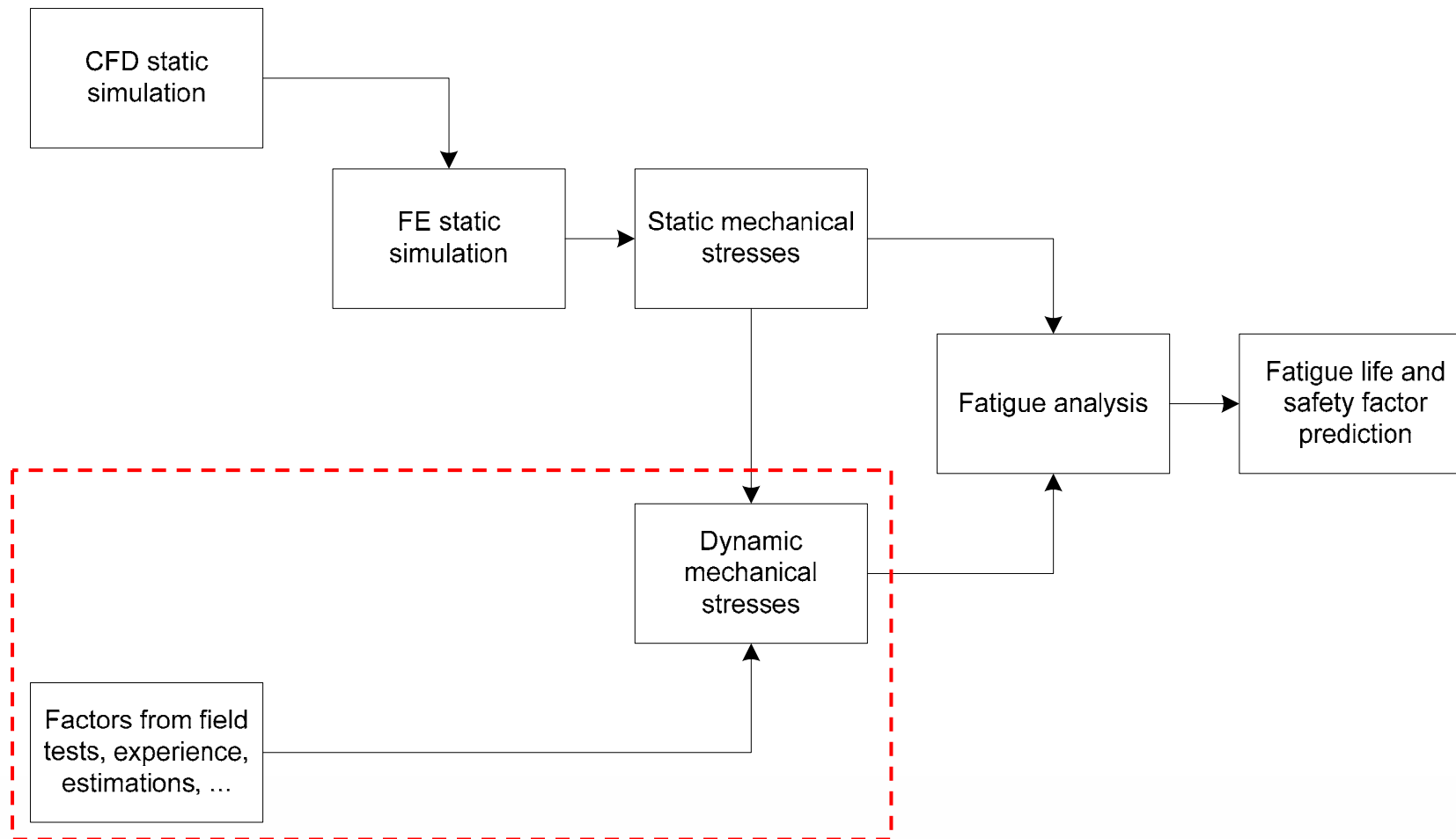


Model

Prototype

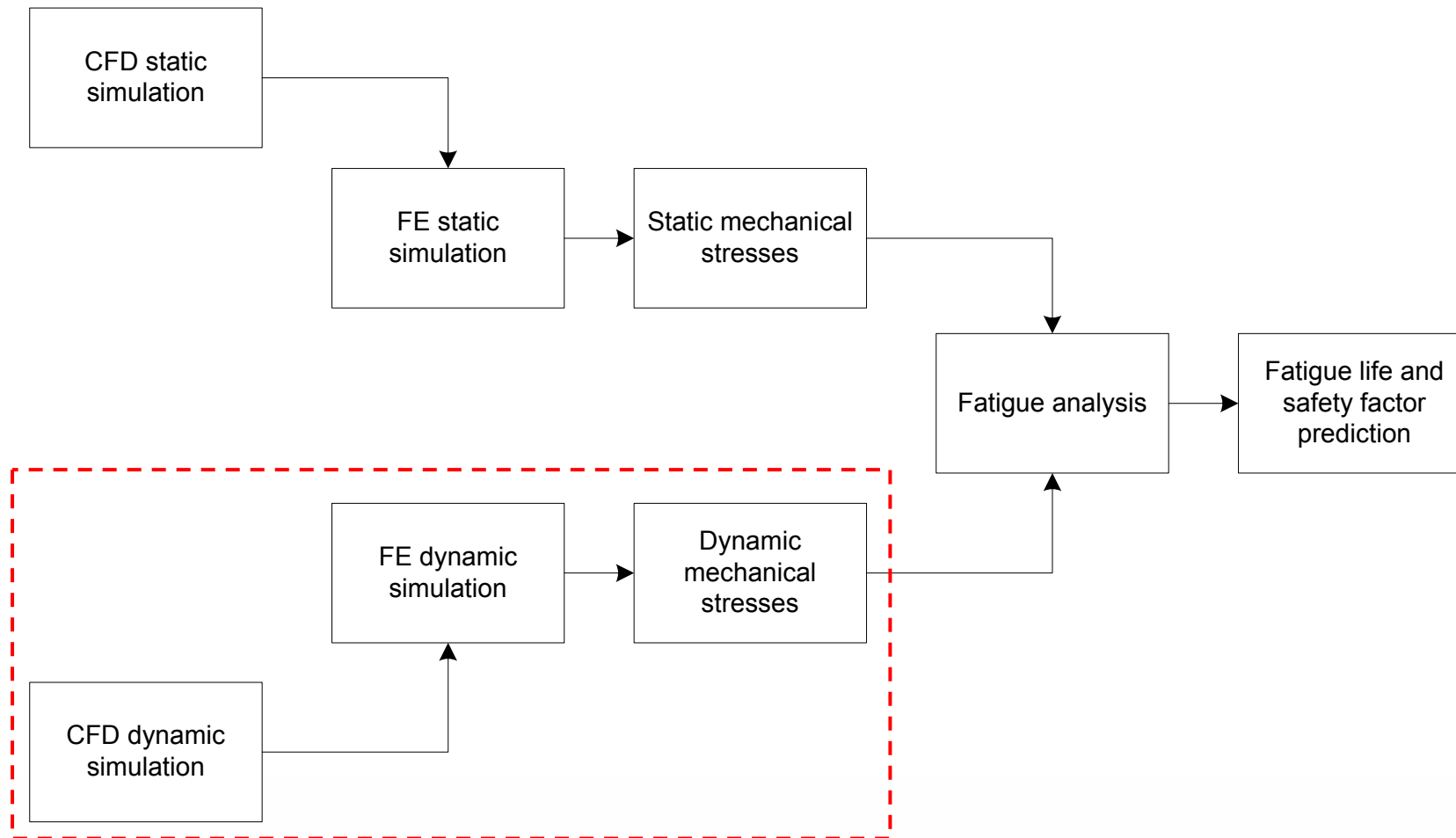


# Problem description – Current procedure

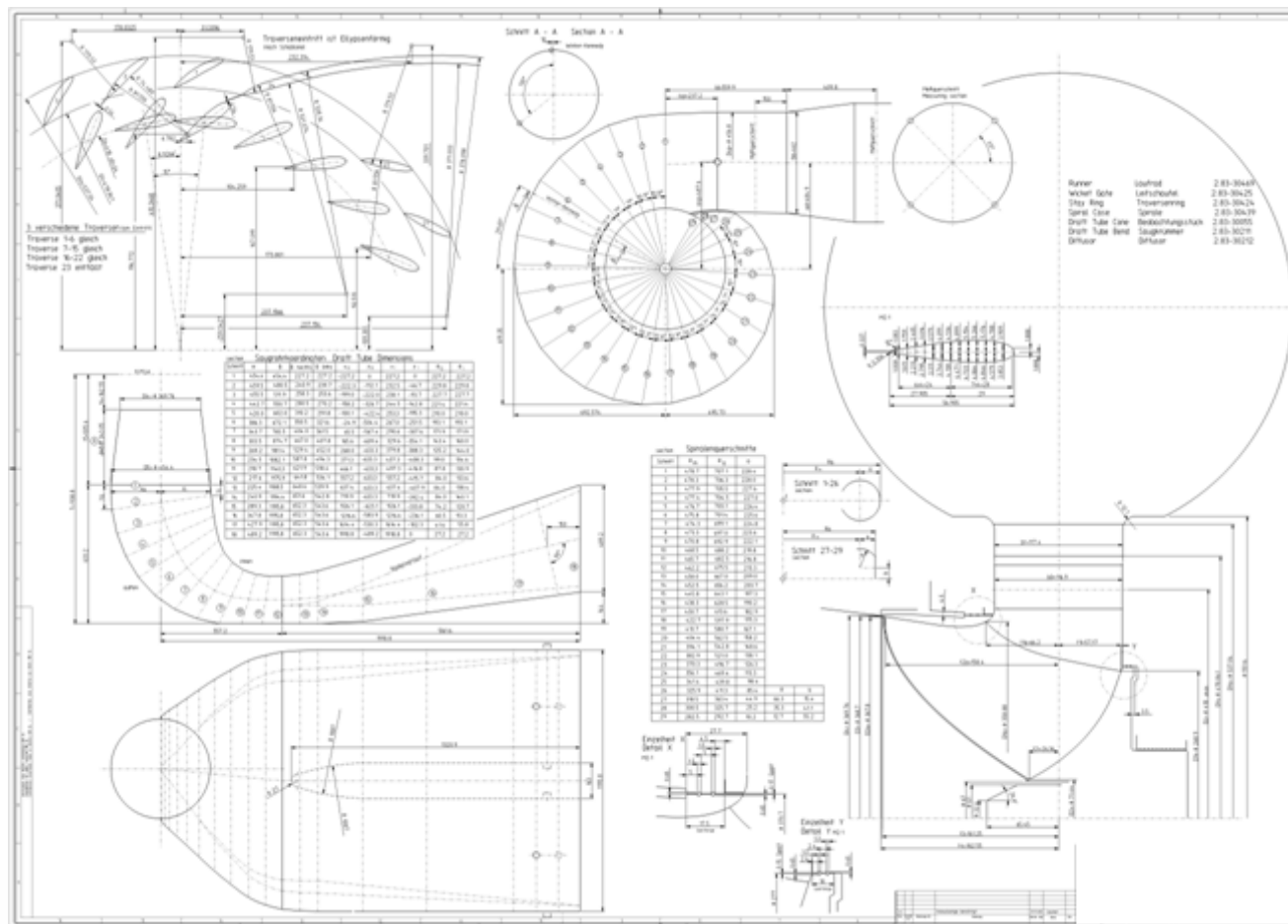




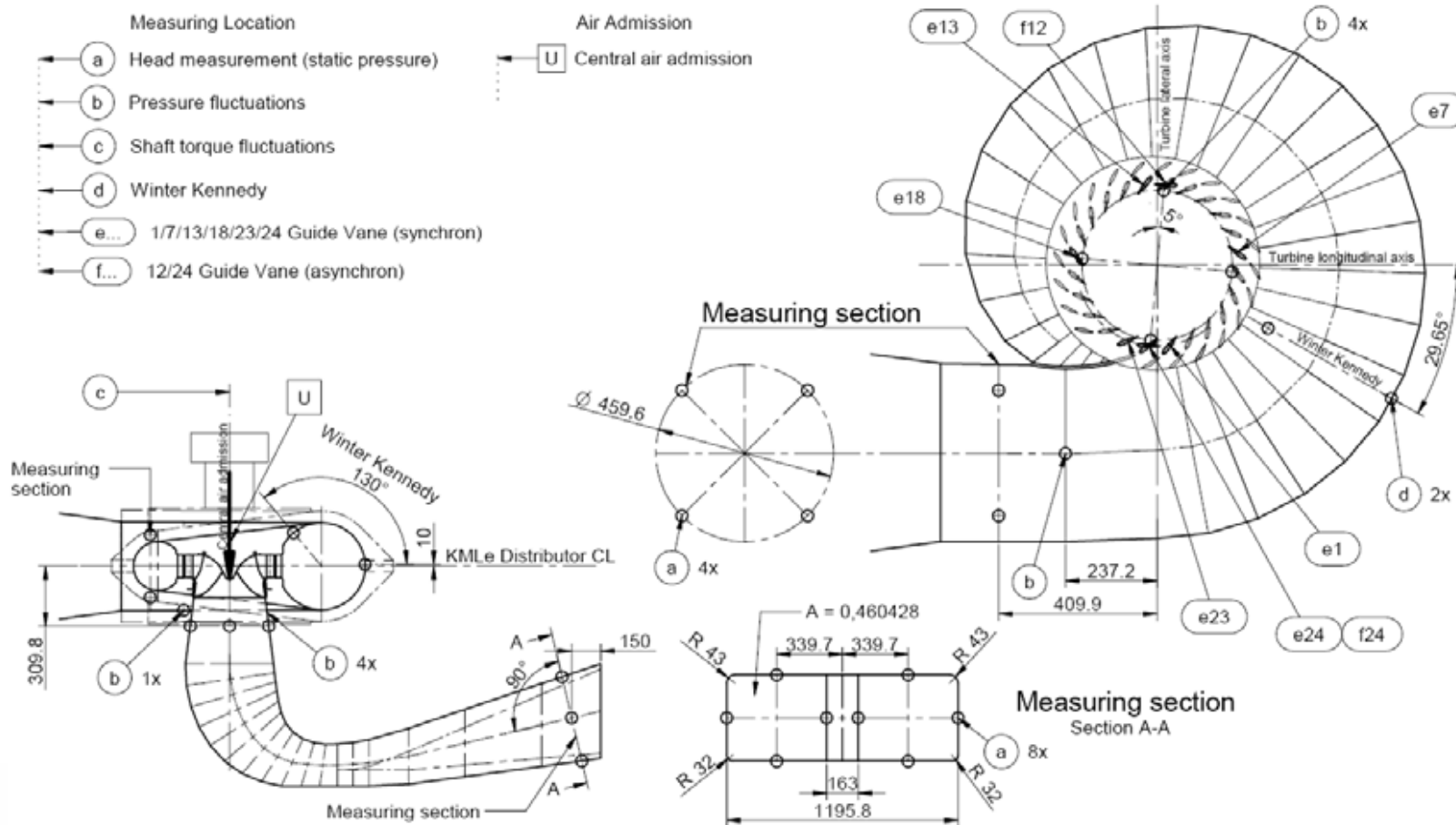
# Problem description – Proposed procedure



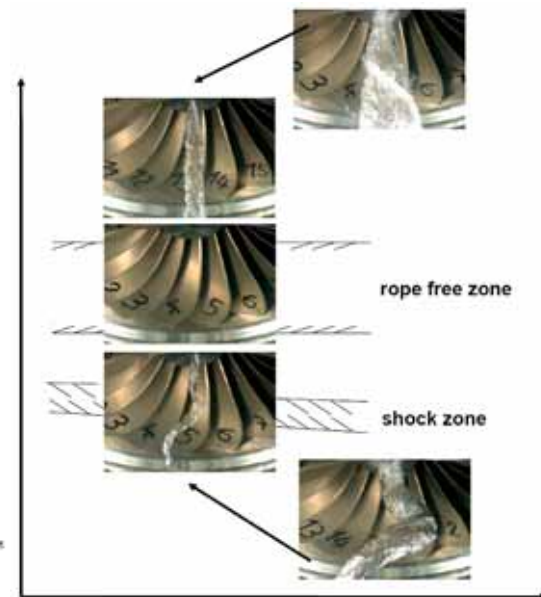
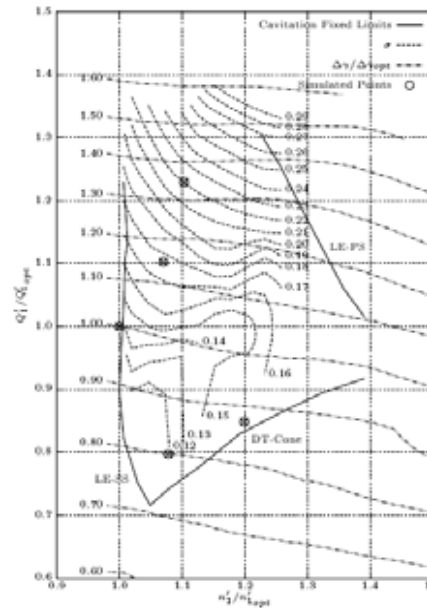
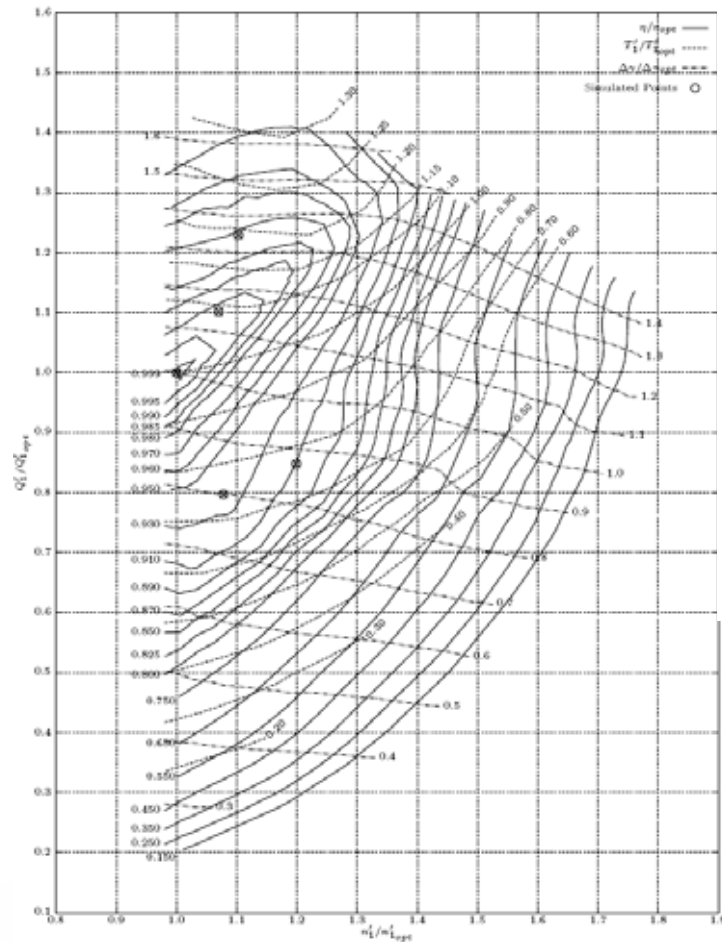
# Machine description – Hydraulic contour



# Machine description – Measuring points



# Machine description – Model hill chart



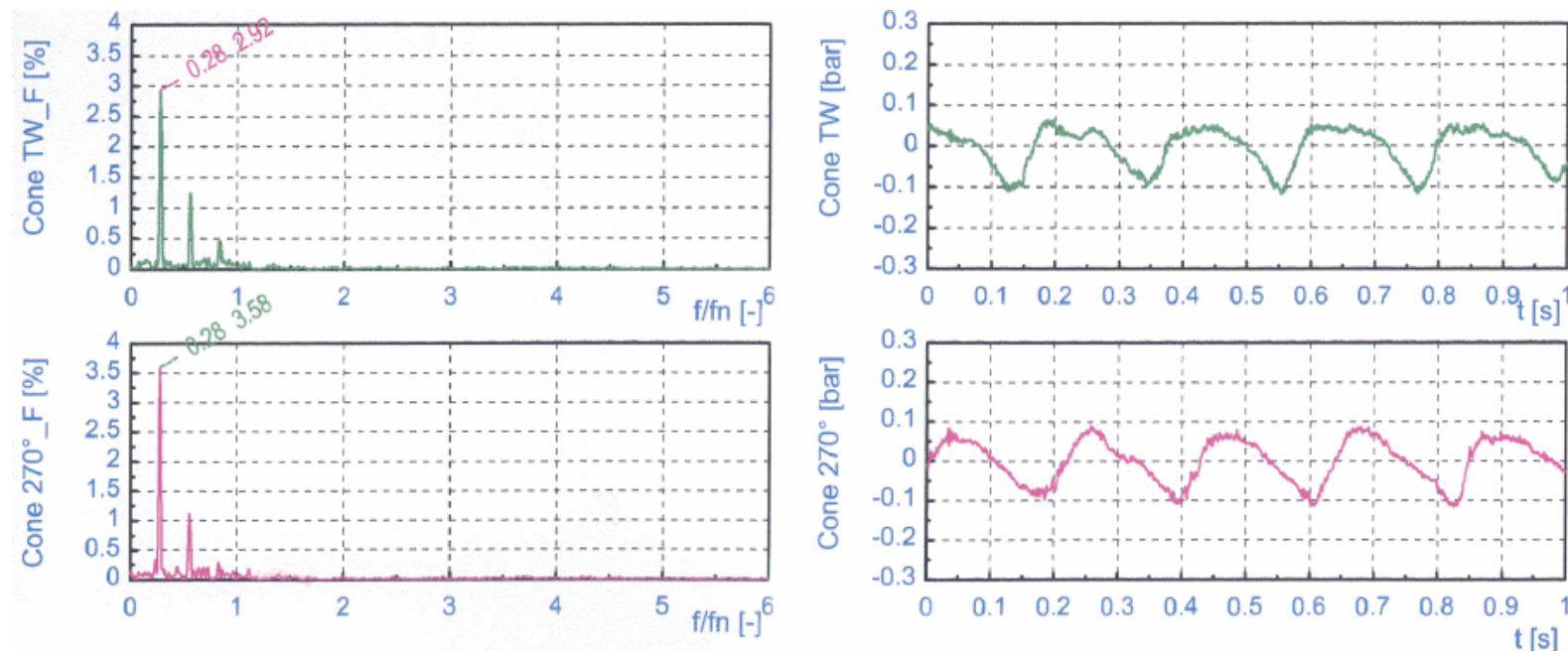
$$n'_1 = nD / \sqrt{H}$$

$$Q'_1 = Q / D^2 \sqrt{H}$$

$$T'_1 = T / D^3 H$$

$$\sigma = (h_{amb} - h_{va} - h_s) / H$$

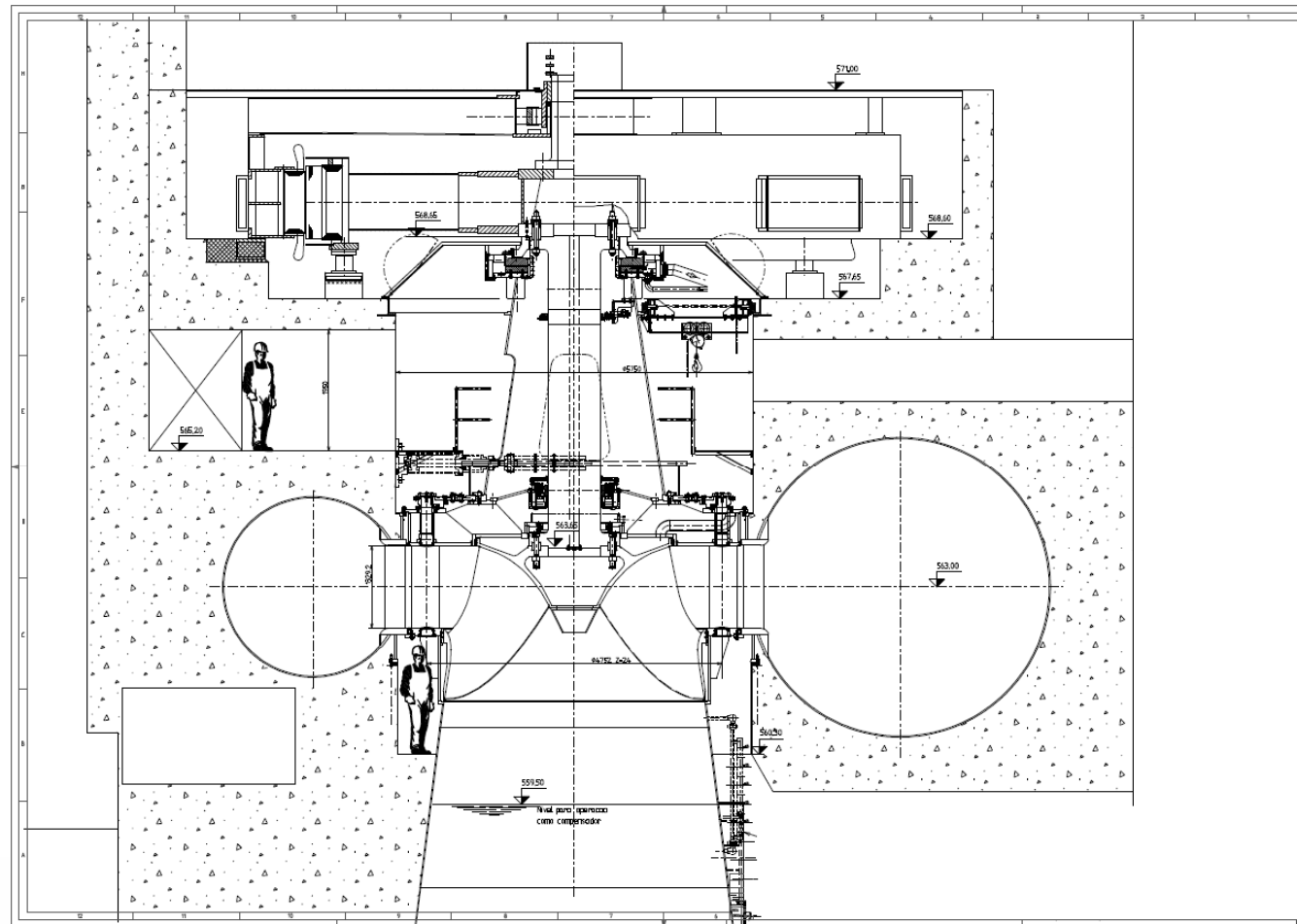
# Machine description – Draft tube oscillations



- Example of pressure fluctuations in the draft tube at part load, measured during the model test:  $(p - \bar{p})/\rho gH$
- Used for calibrating the CFD transient simulation.



# Machine description – Cross-section

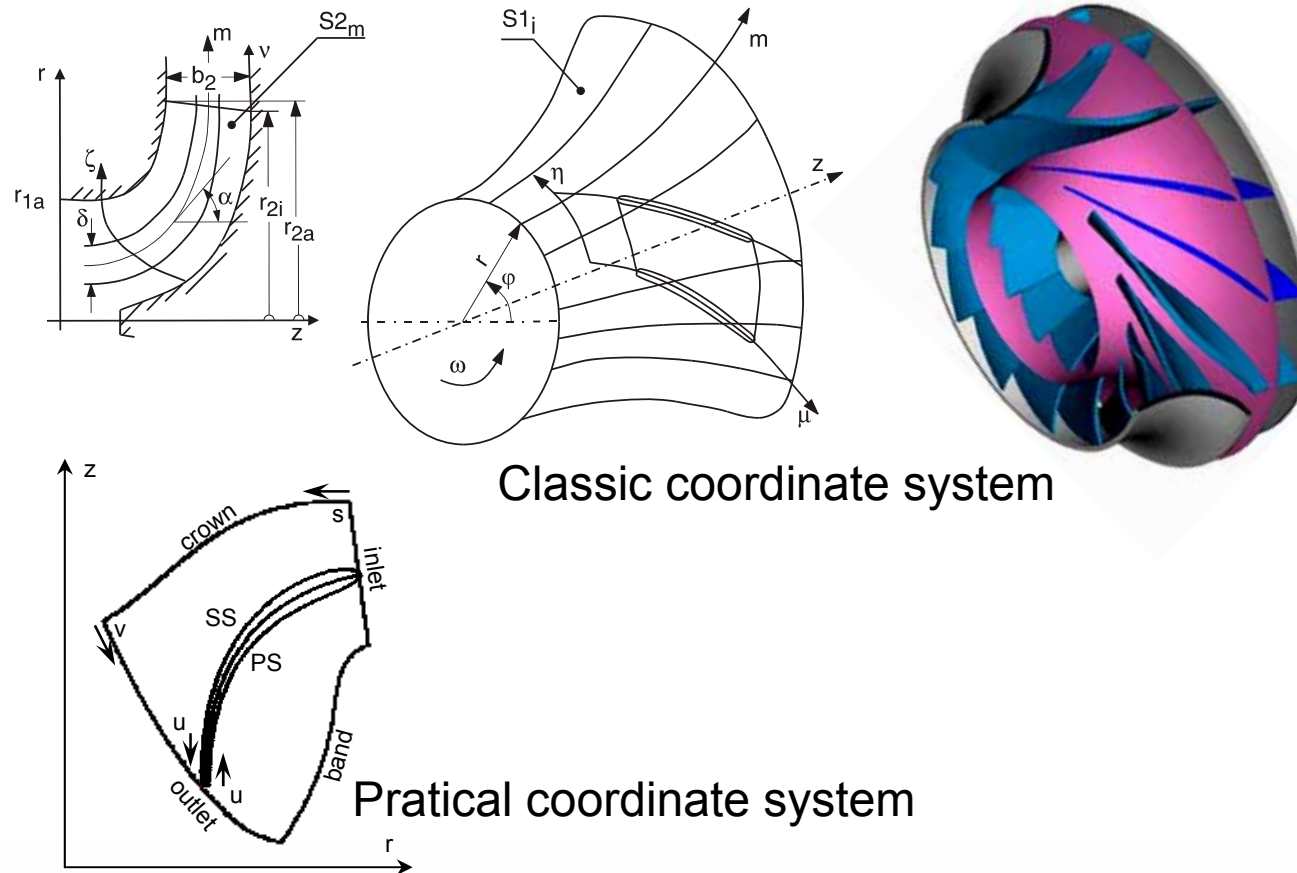


# Machine description – Prototype runner



Prototype runner at the manufacturing shop.

# Machine description – Coordinate system





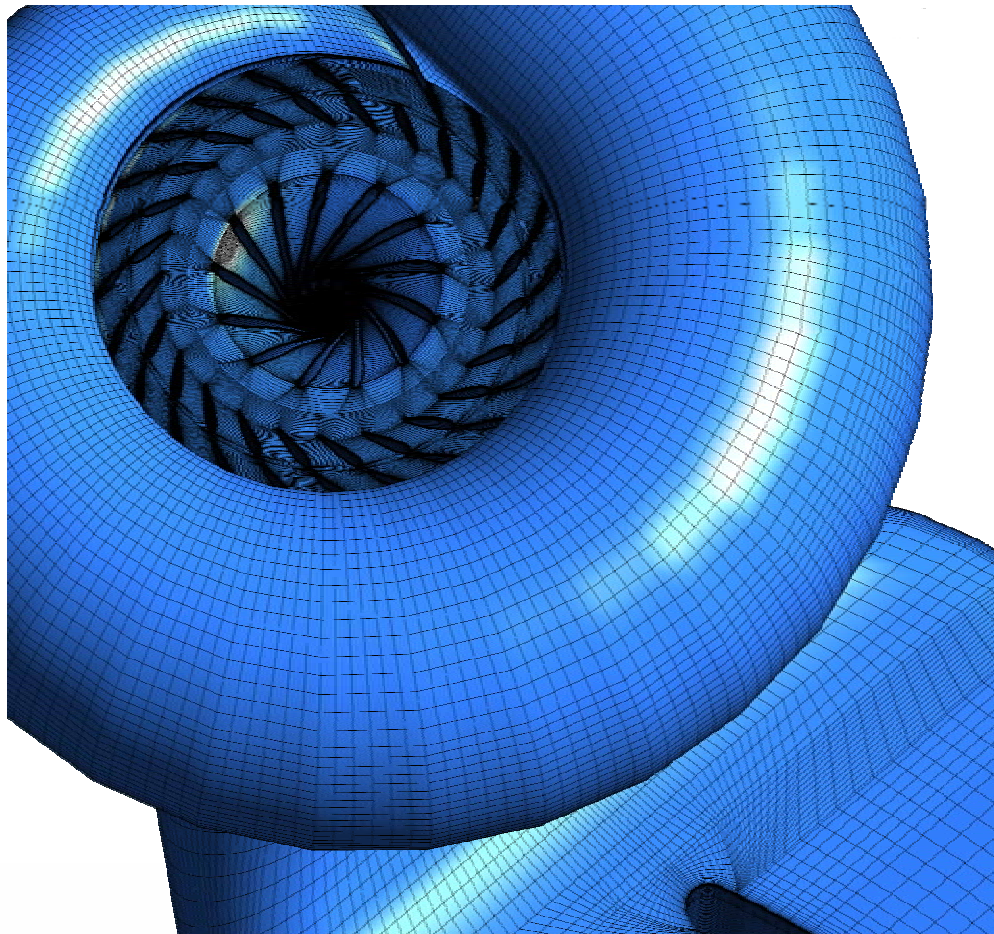
## Numerical set-up – Overview

- Simulation of real Francis turbine:  $n_q = 80 \text{ min}^{-1}$
- Transient CFD simulation
- Complete turbine simulation
- Coupled simulation of all components
- Rotating and non-matching interfaces
- Blading meshed with IDS
- SC and DT meshed with ICEM
- Compared solvers : NS3D, CFX

## Numerical set-up – Tested parameters

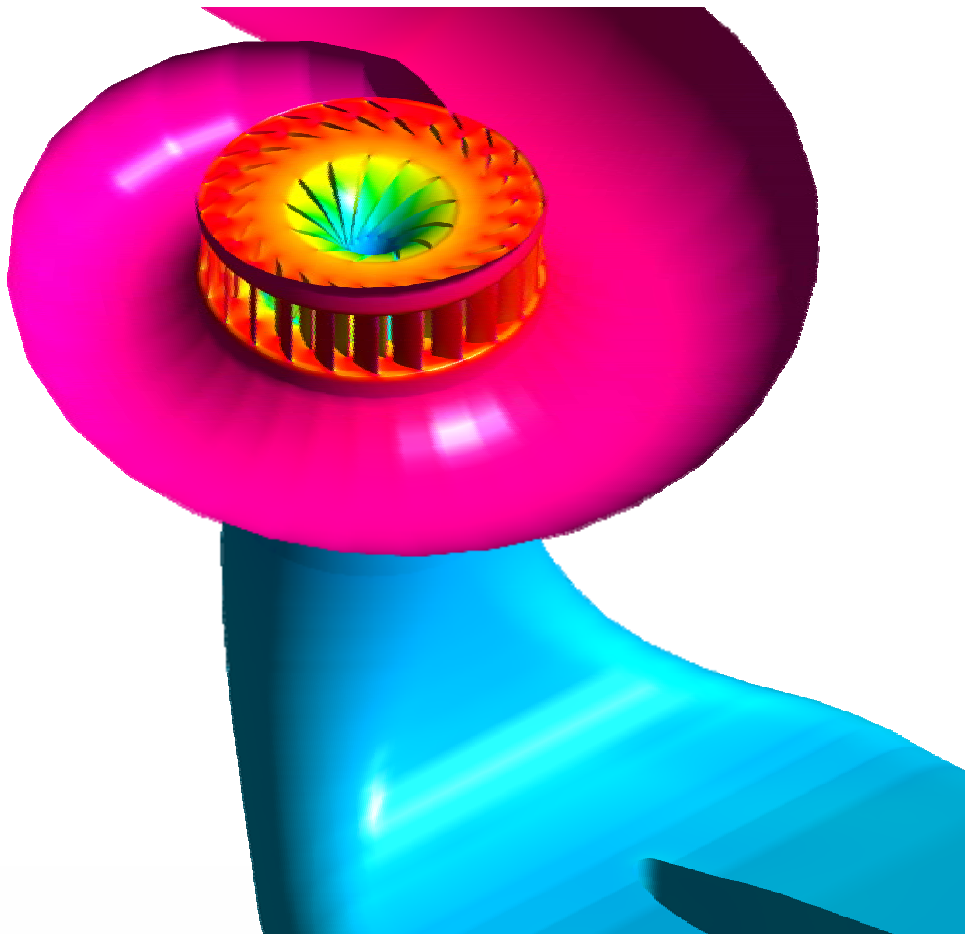
- Mesh density: from  $\sim 3,8$  up to  $\sim 6,0$  million cells
- Interpolation schemes: UDS, CDS, QUICK, MINMOD
- Turbulence models:  $k$ - $\varepsilon$ ,  $k$ - $\varepsilon$  LCL,  $k$ - $\omega$ ,  $k$ - $\omega$  SST
- Turbulence models: URANS, SAS, DES
- Turbulence inlet content: from 1% up to 10%
- Wall treatment: with wall function,  $30 < y^+ < 300$
- Outlet domain extension and BC type

# Numerical set-up – Computational model



Francis turbine  
mesh containing  
~ 6.000.000 cells

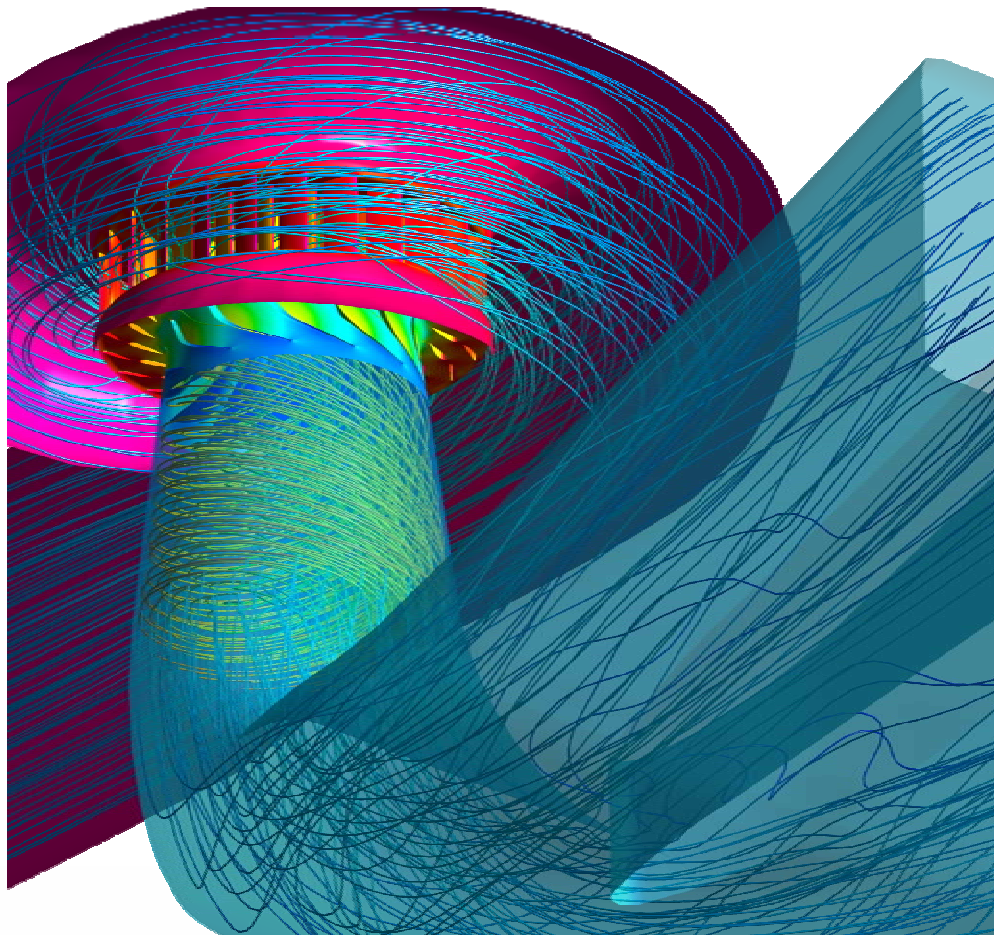
# Numerical set-up – Computational model



Time averaged  
pressure distribution  
at the rated point

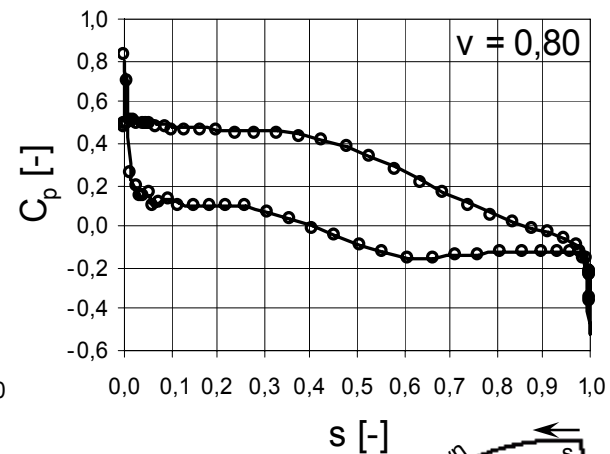
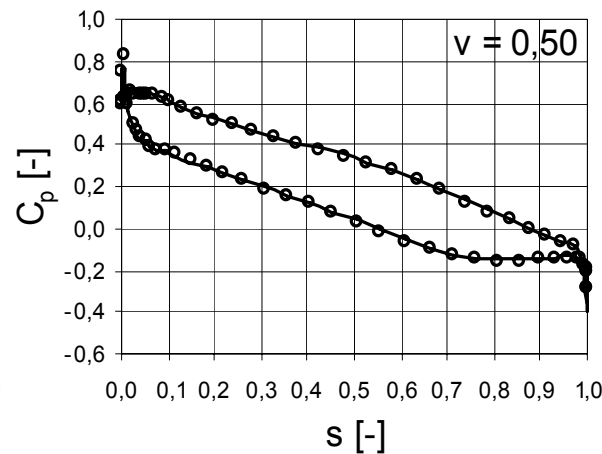
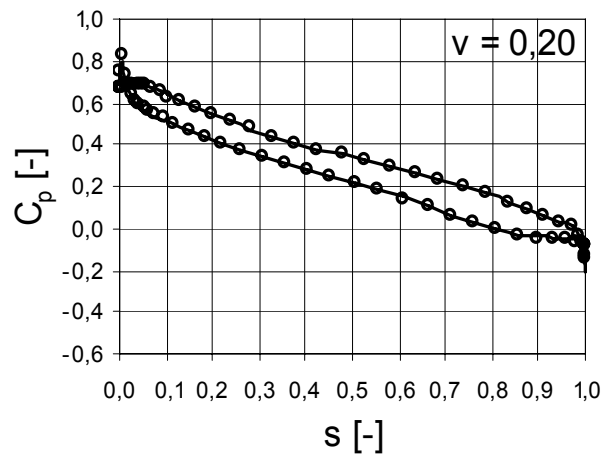


# Numerical set-up – Computational model



Time averaged  
stream lines at the  
rated point

# Numerical set-up – Codes: NS3D & CFX

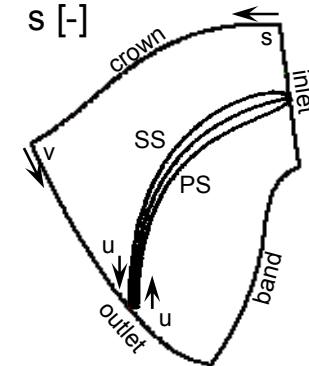


Calculated with NS3D (—) and CFX (○)

$C_p$  : Pressure coefficient

$s$  : Normalized blade length, measured from blade nose

$v$  : Conformal plane coordinate, measured from crown to band



# Numerical set-up – Validation

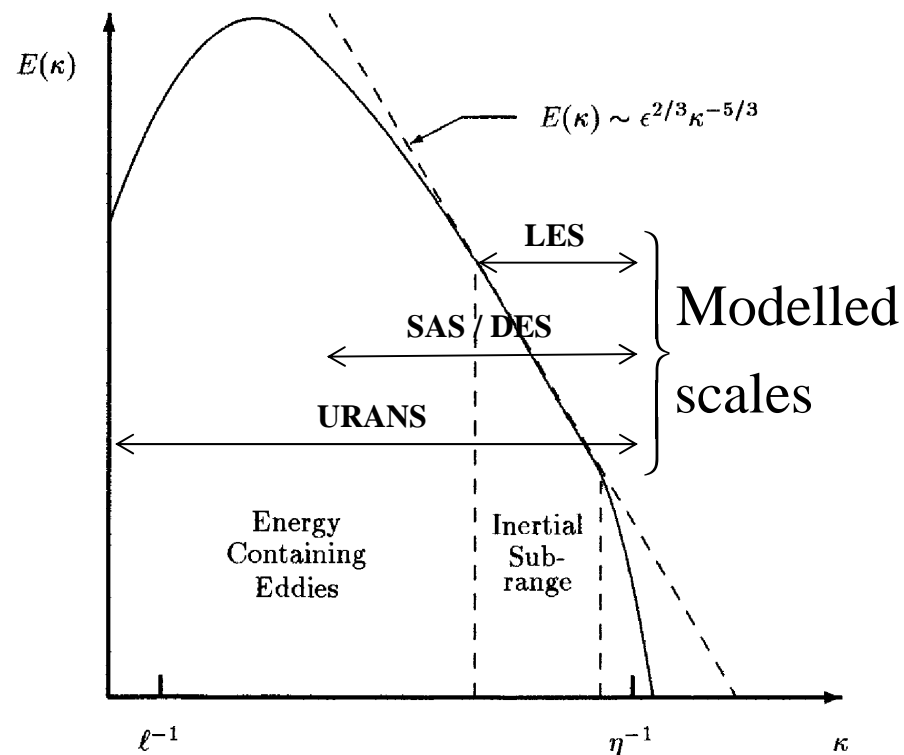
Operating Point	Model Test				Simulation				Deviation			
	$n_1'/n_{1opt}'$	$Q_1'/Q_{1opt}'$	$T_1'/T_{1opt}'$	$\eta/\eta_{opt}$	$n_1'/n_{1opt}'$	$Q_1'/Q_{1opt}'$	$T_1'/T_{1opt}'$	$\eta/\eta_{opt}$	$\delta n_1'$	$\delta Q_1'$	$\delta T_1'$	$\delta \eta$
	[%]	[%]	[%]	[%]	[%]	[%]	[%]	[%]	[%]	[%]	[%]	[%]
Optimum	100,0	100,0	100,0	100,0	99,4	100,0	100,3	100,2	<b>-0,6</b>	<b>&lt; 0,1</b>	<b>0,3</b>	<b>0,2</b>
Rated (design pt.)	110,3	111,5	108,3	97,2	109,6	111,5	110,0	98,7	<b>-0,6</b>	<b>&lt; 0,1</b>	<b>1,6</b>	<b>1,5</b>
Normal	107,0	103,0	102,2	99,3	106,0	103,0	102,4	99,4	<b>-1,0</b>	<b>&lt; 0,1</b>	<b>0,2</b>	<b>0,1</b>
Part load at high head	107,8	73,9	69,3	93,8	106,7	73,9	69,3	93,8	<b>-1,0</b>	<b>&lt; 0,1</b>	<b>0,0</b>	<b>0,0</b>
Part load at low head	119,9	70,8	64,4	91,0	119,0	70,8	65,1	91,9	<b>-0,7</b>	<b>&lt; 0,1</b>	<b>1,0</b>	<b>1,0</b>

## Transient simulation set-up – Parameters

- Number of time steps (TS) for capturing:
  - DTI: ~ 120 TS / Revolution (Courant number  $\leq 30$ )
  - RSI: ~ 400 TS / Revolution (Courant number  $\leq 1,5$ )
  - VSE: ~ 6000 TS / Revolution (Courant number  $\leq 0,2$ )
- Required number of revolutions until stabilization:
  - ~ 35 at the rated operating point
- Cluster: 8 quad-core Intel Q6600 2,4GHz, 2GB RAM
- Computation speed: ~ 2 revolutions / day (for RSI)
- Solver: BCGSTAB without multigrid approach



# Transient simulation set-up – Turbulence



- Kolmogorov length scale:
  - In URANS, all the eddies are modelled.
  - In DNS, all the eddies are numerically computed.
  - In LES, the biggest eddies, i.e. the most energetic, are computed, and the smallest are modelled.
  - DES and SAS represent a compromise between URANS and LES.

# Transient simulation set-up – Validation

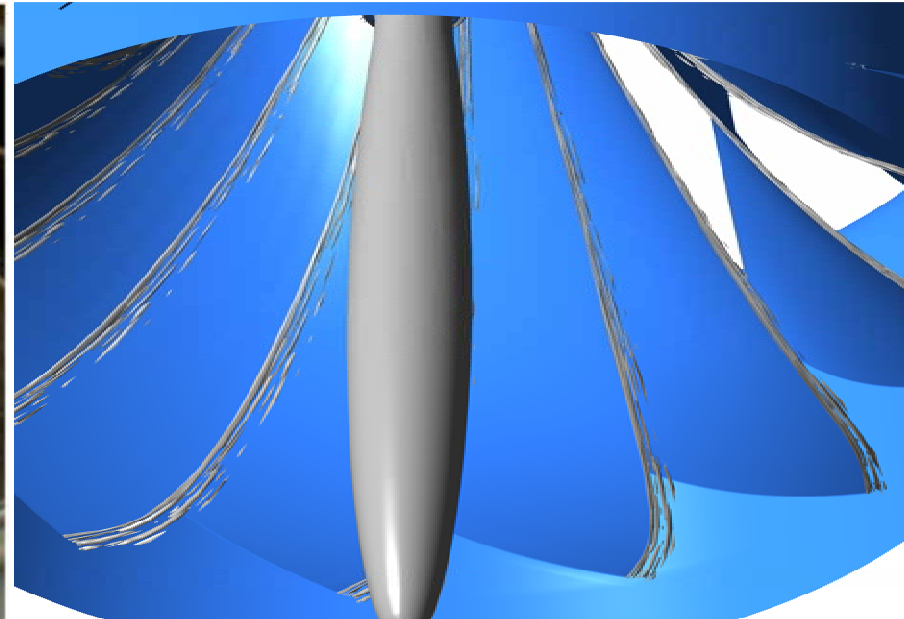
- Peak to peak pressure oscillation at the draft tube cone: ( $\Delta p = p - \bar{p}$ ,  $\Delta p_{P2P} = \Delta p_{\max} - \Delta p_{\min}$ )

Part load at low head	$\frac{\Delta p_{P2P}^{HW}}{\rho g H}$ [%]	$\frac{\Delta p_{P2P}^{90^\circ}}{\rho g H}$ [%]	$\frac{\Delta p_{P2P}^{TW}}{\rho g H}$ [%]	$\frac{\Delta p_{P2P}^{270^\circ}}{\rho g H}$ [%]	$\frac{f}{f_n}$ [-]
Model Test	10,58	9,02	11,42	13,56	0,295
Simulation	10,08	8,60	11,88	13,10	0,315
<b>Deviation</b>	<b>-0,50</b>	<b>-0,42</b>	<b>0,46</b>	<b>-0,46</b>	<b>6,8%</b>

# Transient simulation – Validation

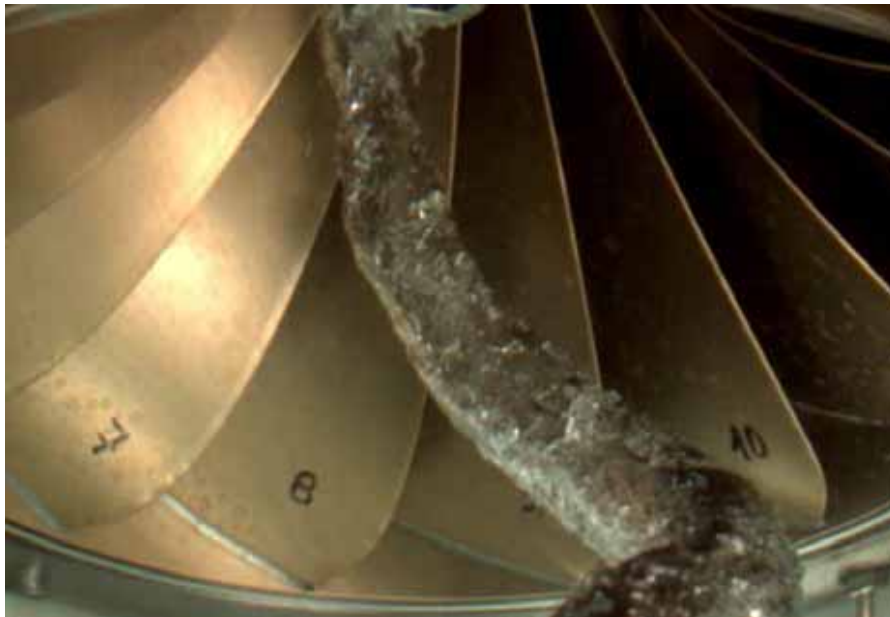


Observed at the model test  
for the rated operating point



Numerically simulated for  
the rated operating point  
(vapour pressure isosurface)

# Transient simulation – Validation



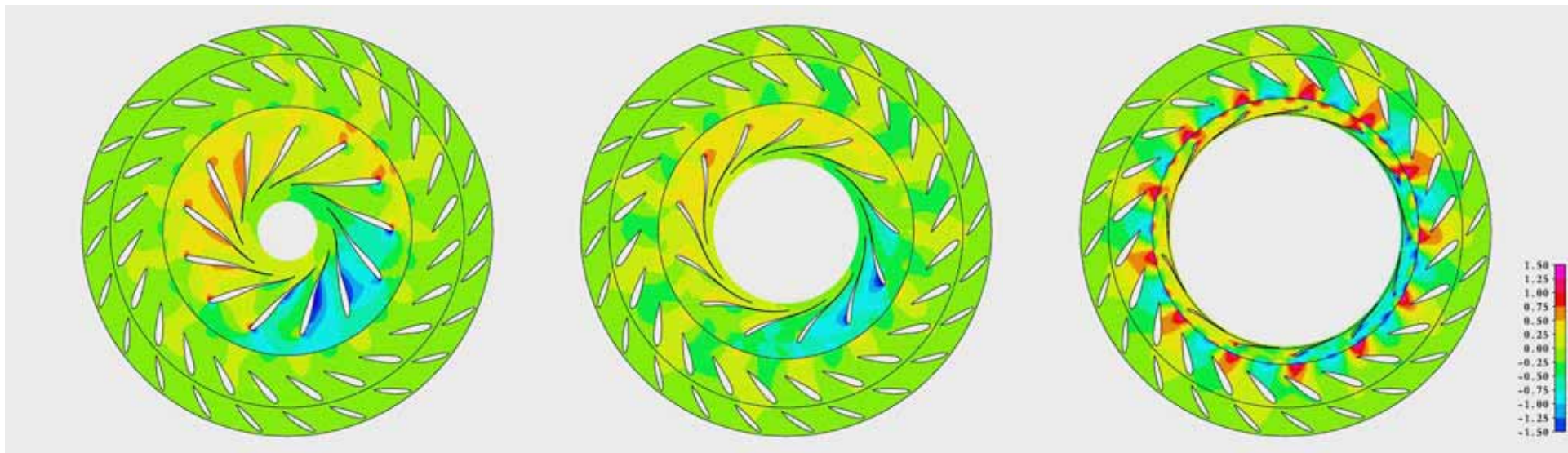
Observed at the model test  
for part load at low head



Numerically simulated for  
part load at low head  
(vapour pressure isosurface)

# Rated point results – Pressure oscillation

- Pressure oscillation,  $\Delta p / \rho g H$  [%], at conformal planes:  
( $\Delta p = p - \bar{p}$ )



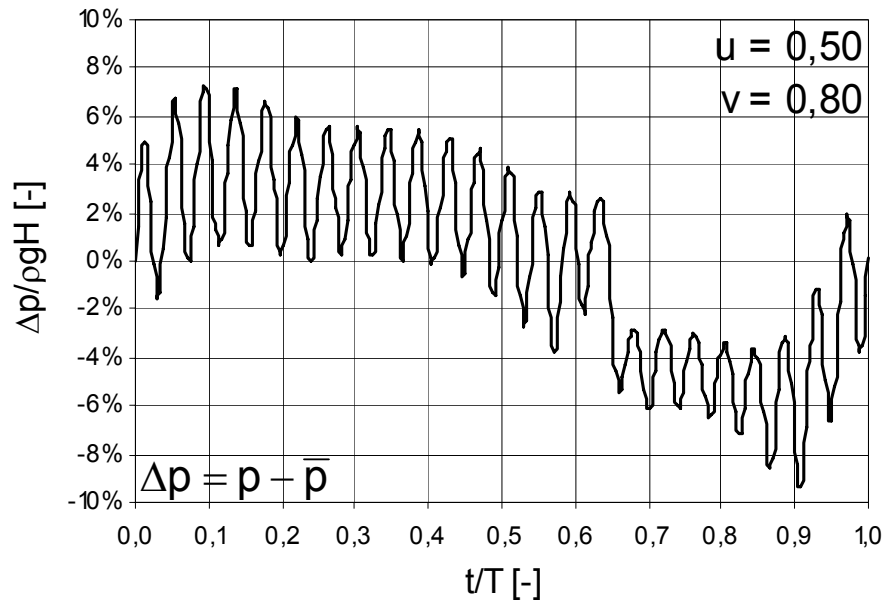
$v = 0,20$

$v = 0,50$

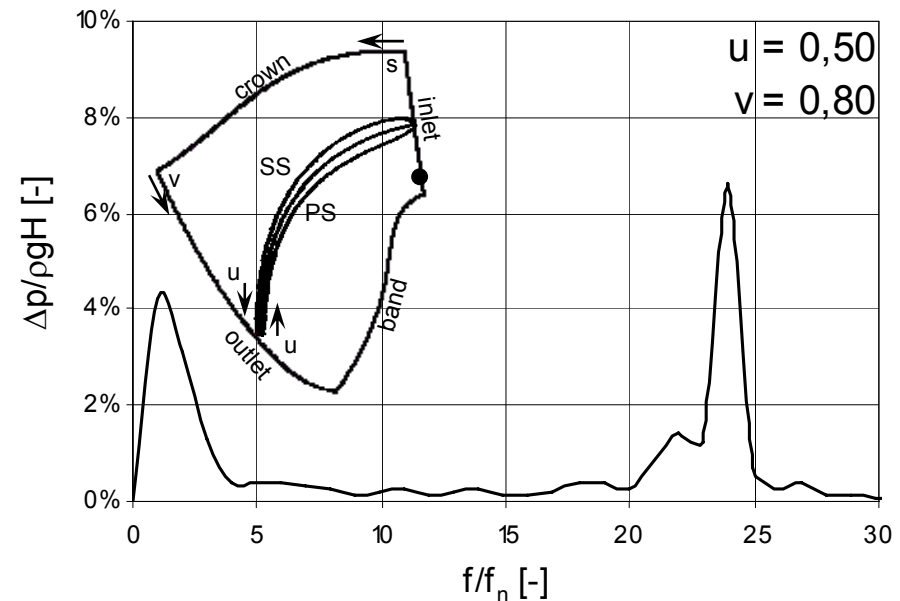
$v = 0,80$



# Rated point results – Time history

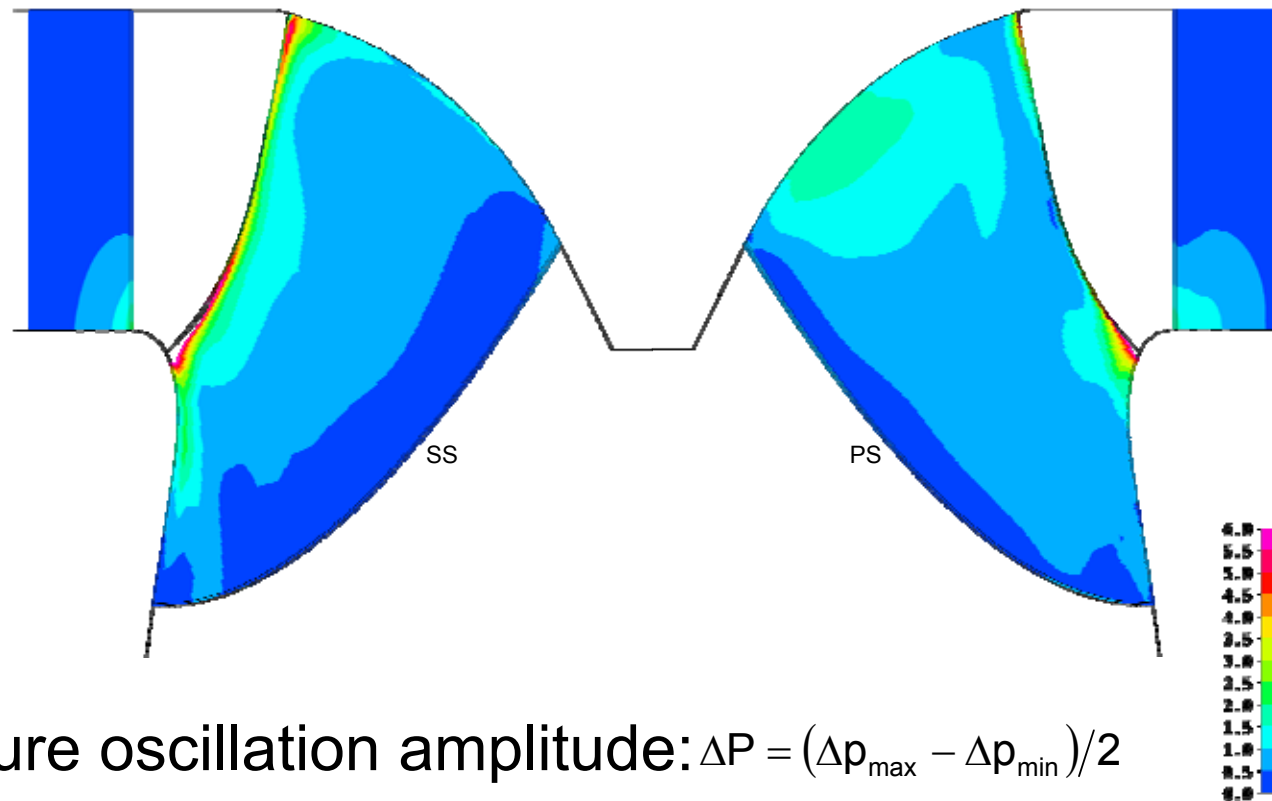


Time history at blade leading edge near to the band



Fourier transform at blade leading edge near to the band

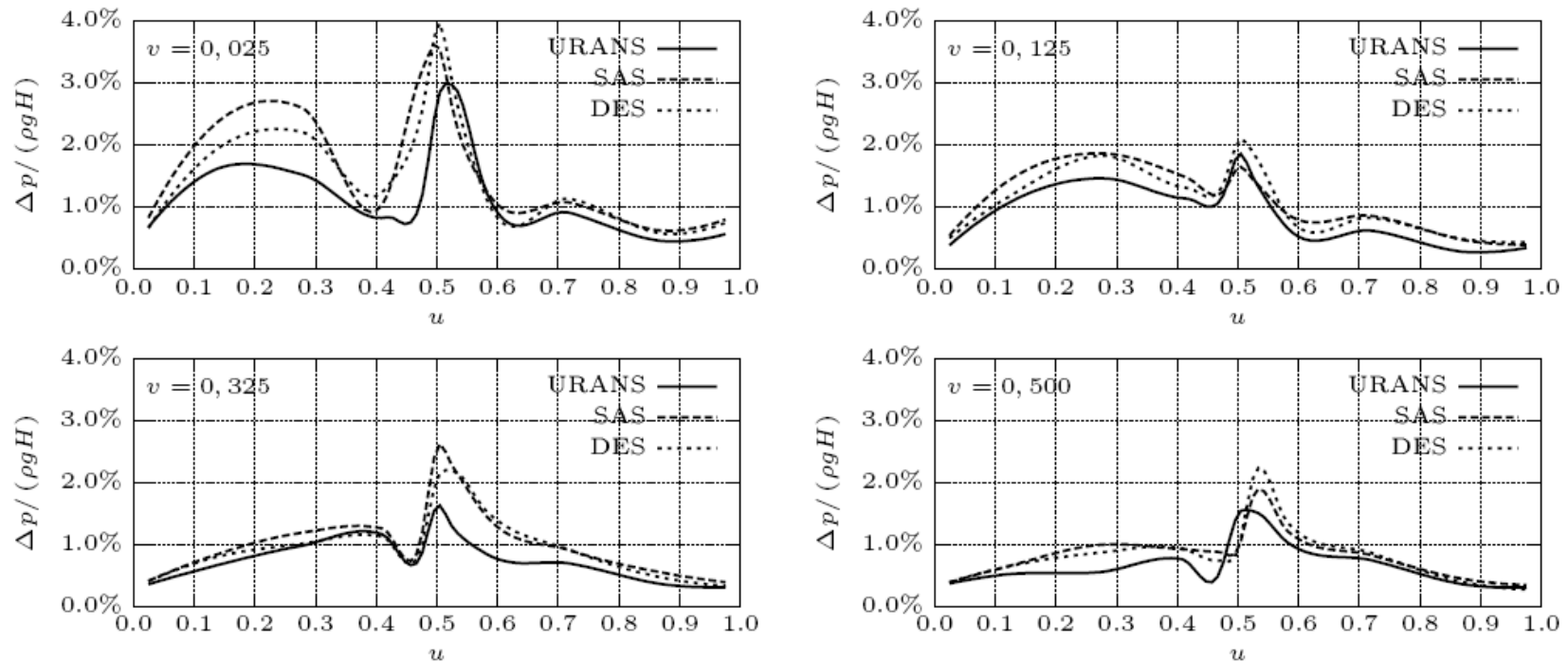
# Rated point results – Oscillation amplitude



Pressure oscillation amplitude:  $\Delta P = (\Delta p_{\max} - \Delta p_{\min})/2$

Meridian view. Values above 6,0% not coloured.

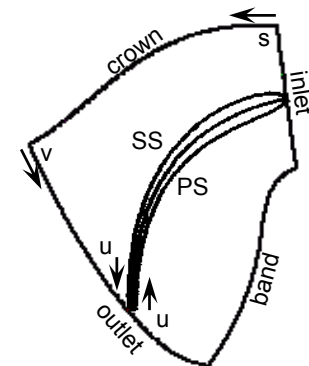
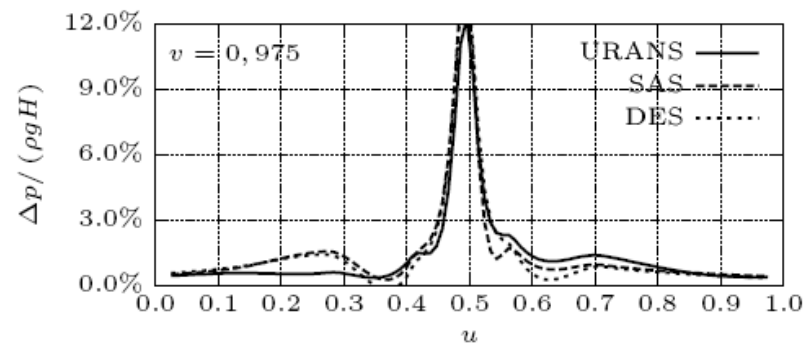
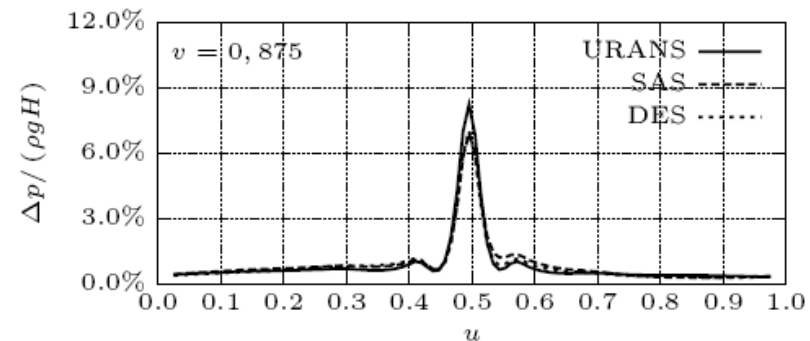
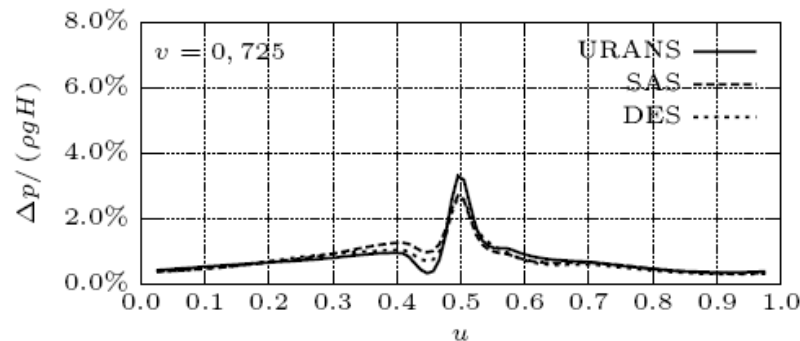
# Rated point results – Oscillation amplitude



## Pressure oscillation amplitude and the turbulence models



# Rated point results – Oscillation amplitude



## Pressure oscillation amplitude and the turbulence models

## Rated point results – Comments

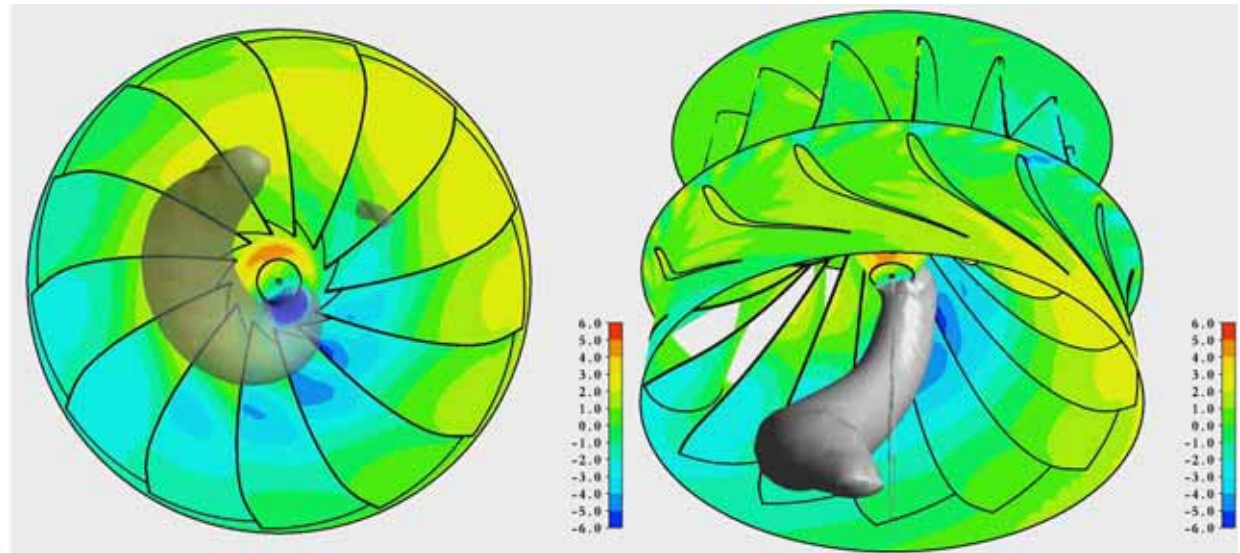
- Flow dominated by kinematic effects from RSI
- Limited influence from turbulence models on results
- Pressure oscillation amplitude:
  - **Maximum:** 12,4% at the leading edge near to band
  - **Overall:** 0,3%-2,1% in most part of the blade
- Dominating frequencies:
  - $f_n$ : Rotation, nose vane passing frequency
  - $f_n \times z_0$ : Guide vanes passing frequency

# Part load results – Pressure oscillation

- Pressure oscillation,  $\Delta p / \rho g H$  [%]: ( $\Delta p = p - \bar{p}$ )



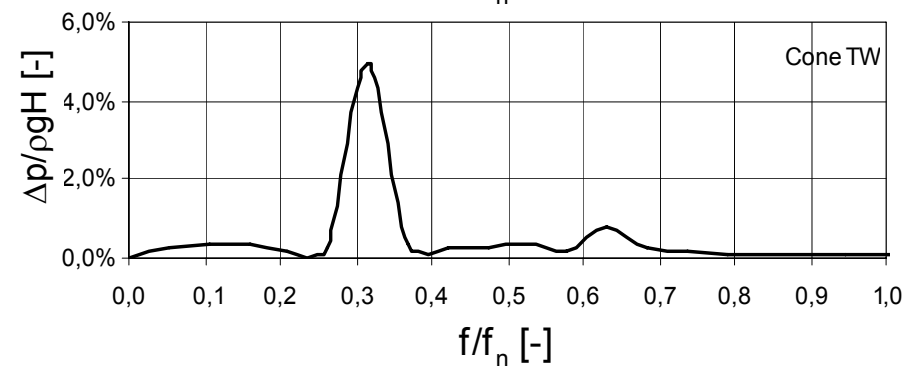
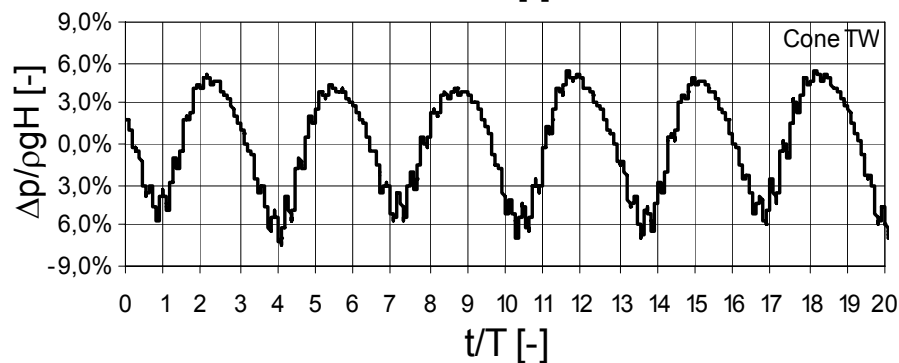
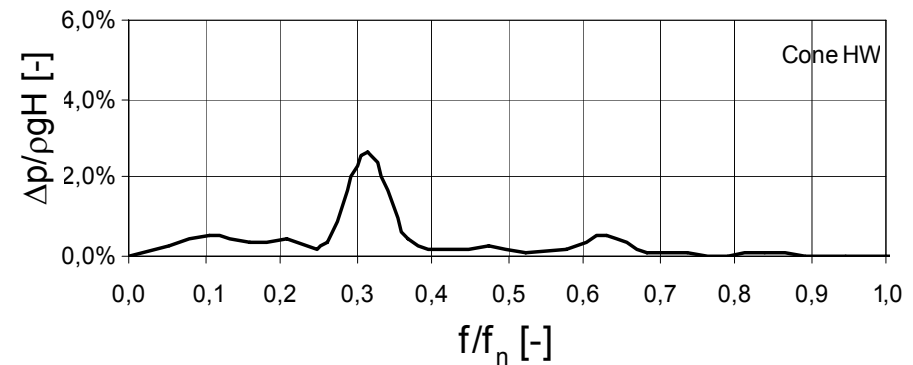
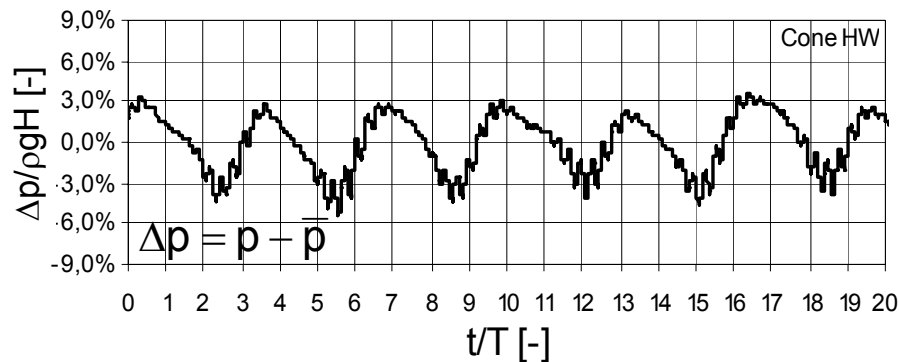
Stationary  
reference



Bottom  
view

Runner  
reference

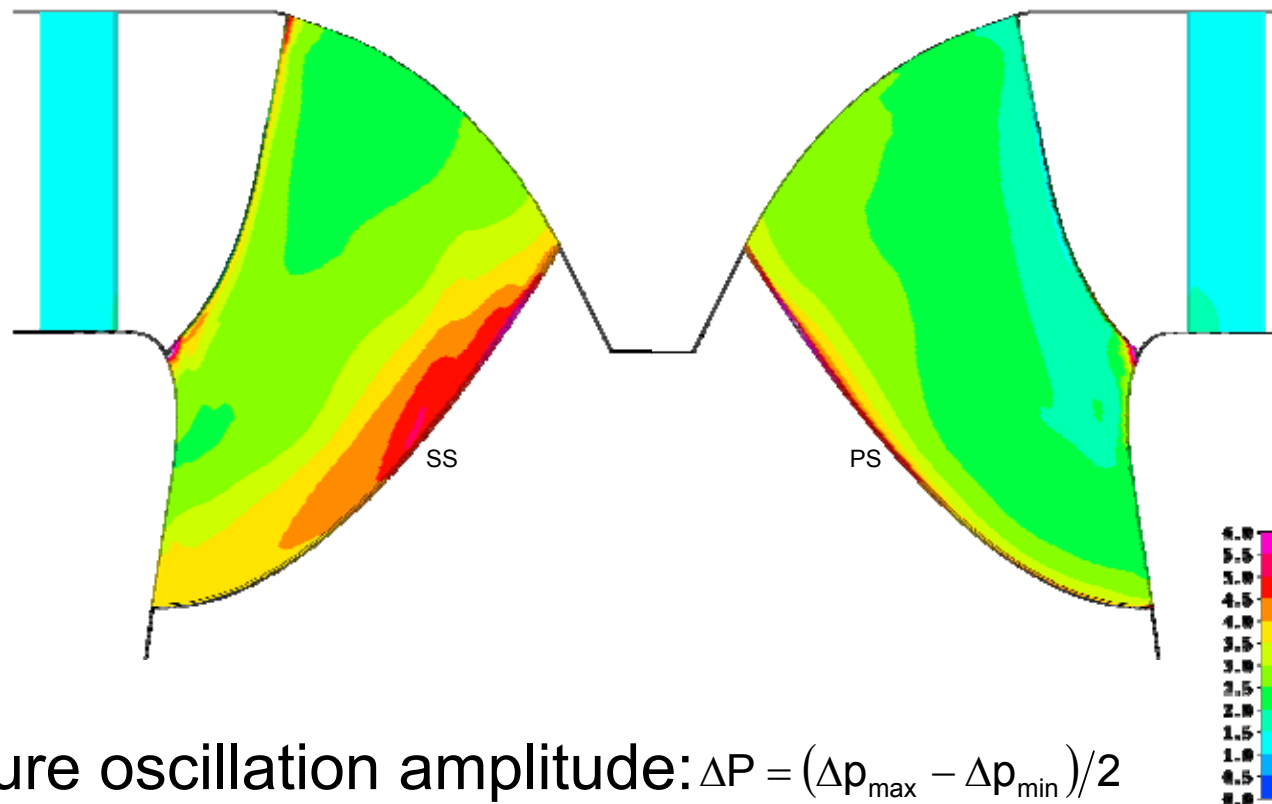
# Part load results – Time history



Time history at draft tube cone

Fourier transform at DT cone

# Part load results – Oscillation amplitude

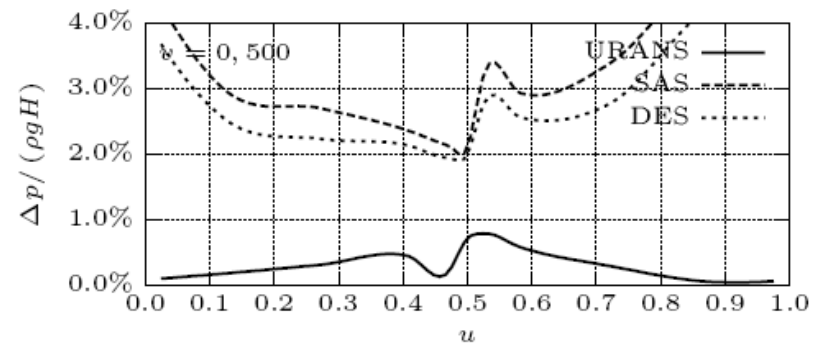
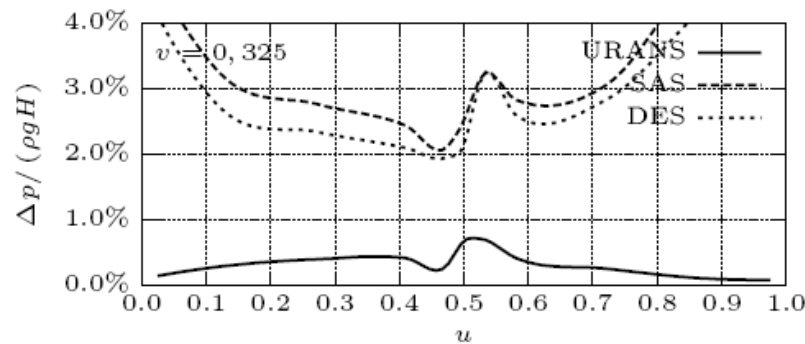
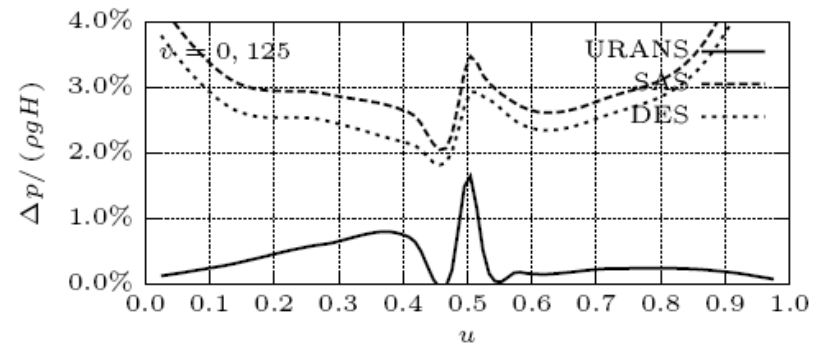
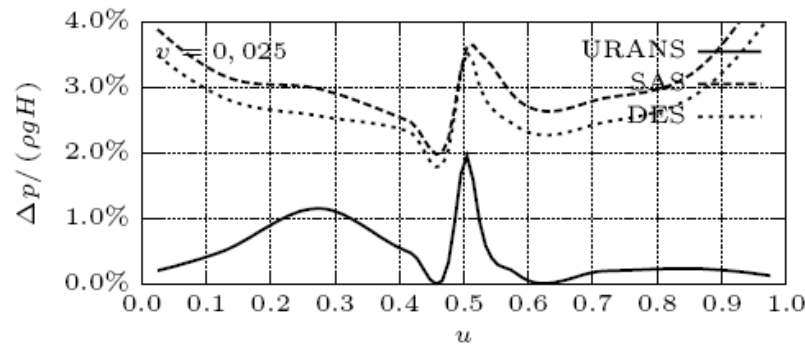


Pressure oscillation amplitude:  $\Delta P = (\Delta p_{\max} - \Delta p_{\min})/2$

Meridian view

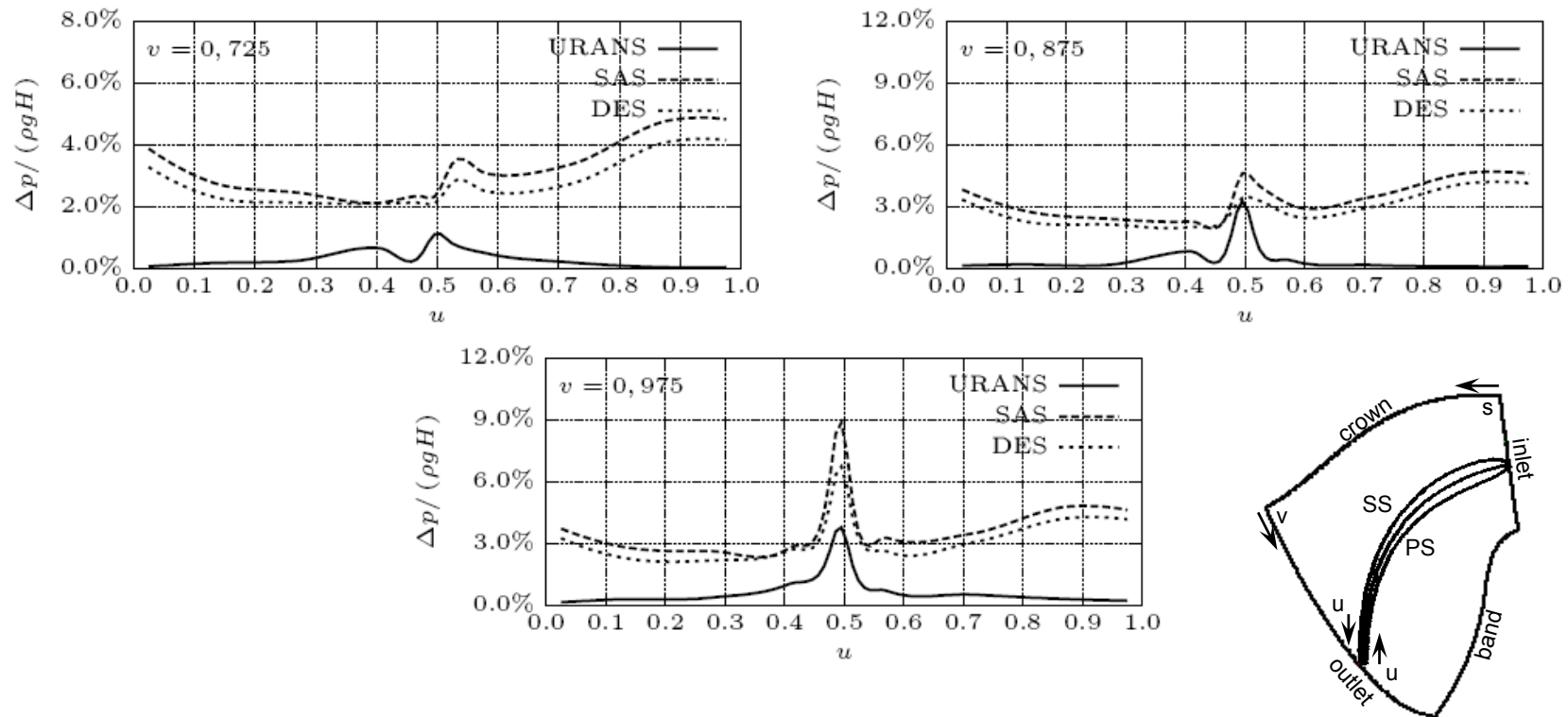


# Part load results – Turbulence models



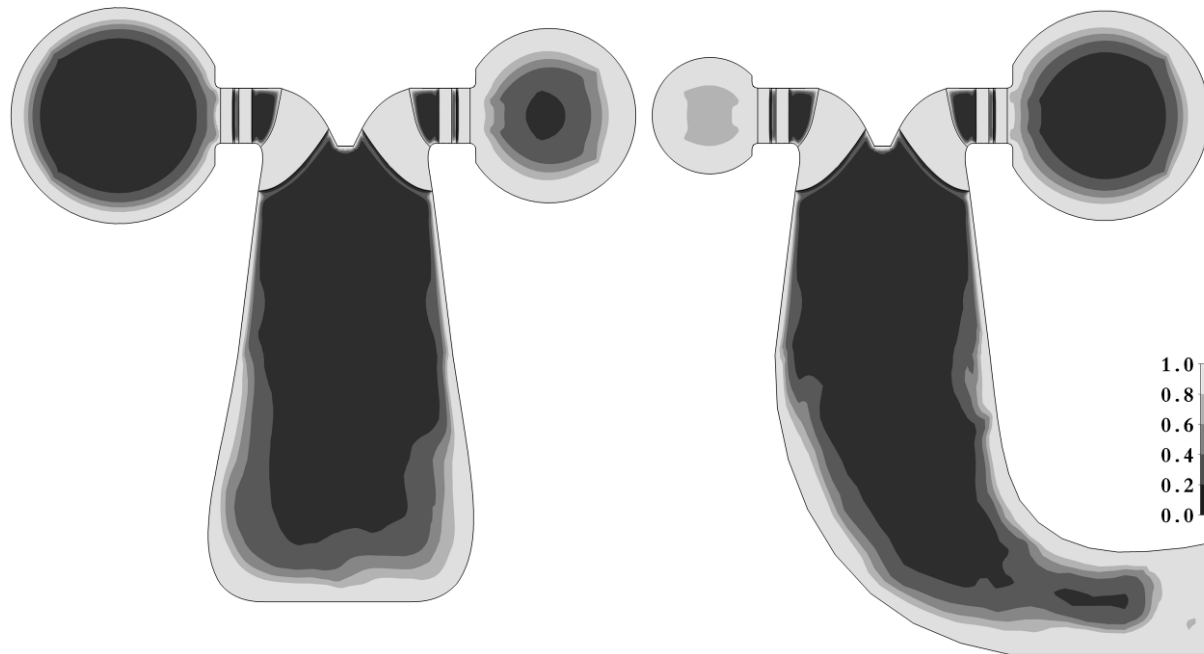
## Pressure oscillation amplitude and the turbulence models

# Part load results – Turbulence models



## Pressure oscillation amplitude and the turbulence models

# Part load results – Blending Function

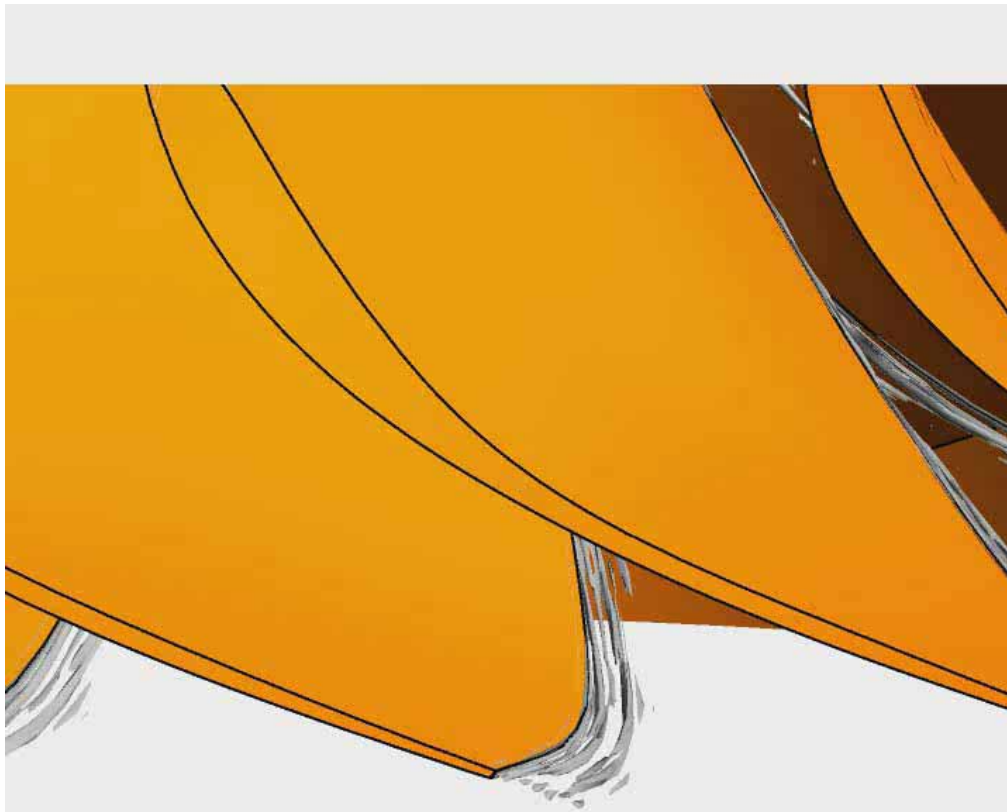


Blending function for DES and SAS  
Transversal and longitudinal views

## Part load results – Comments

- URANS cannot capture the DTI effects
- Turbulence models such as SAS, DES or LES are needed
- Pressure oscillation amplitude:
  - URANS: 3,9% (leading edge) / 0,1%-1,2% (blade)
  - SAS: 5,0% (leading edge) / 0,6%-5,0% (blade)
- Dominating frequency:
  - $0,32 \cdot f_n$ : Draft tube vortex rope rotating frequency

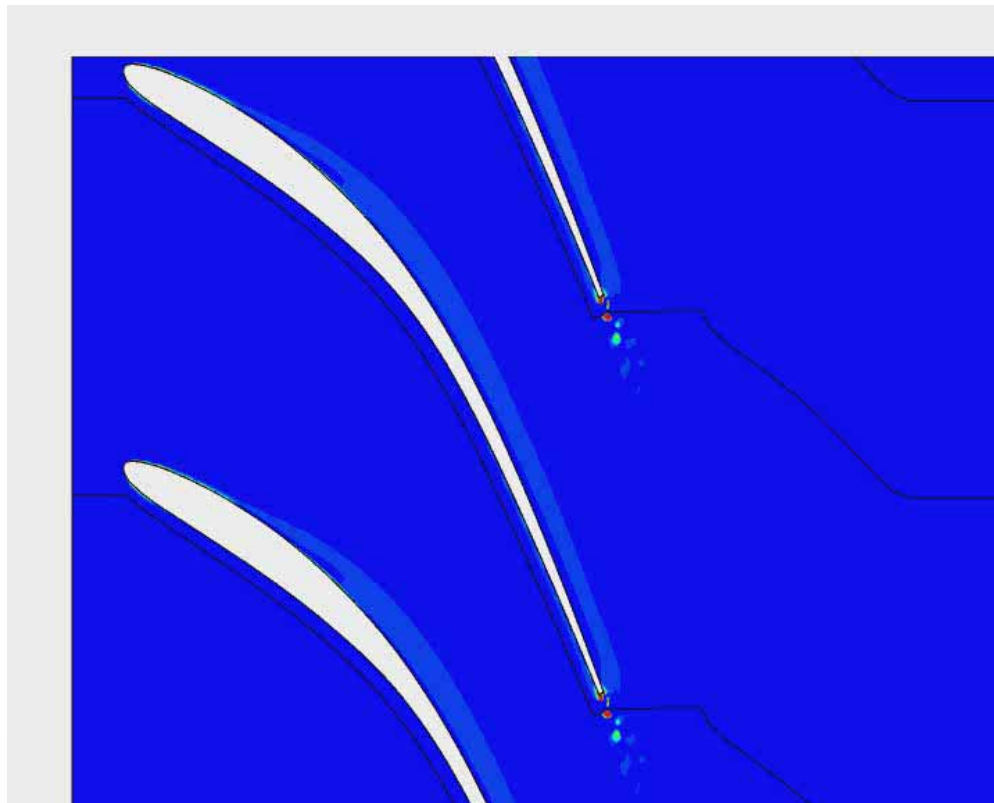
# Rated point results – Vortex shedding



Vortex shedding at  
runner trailing edge

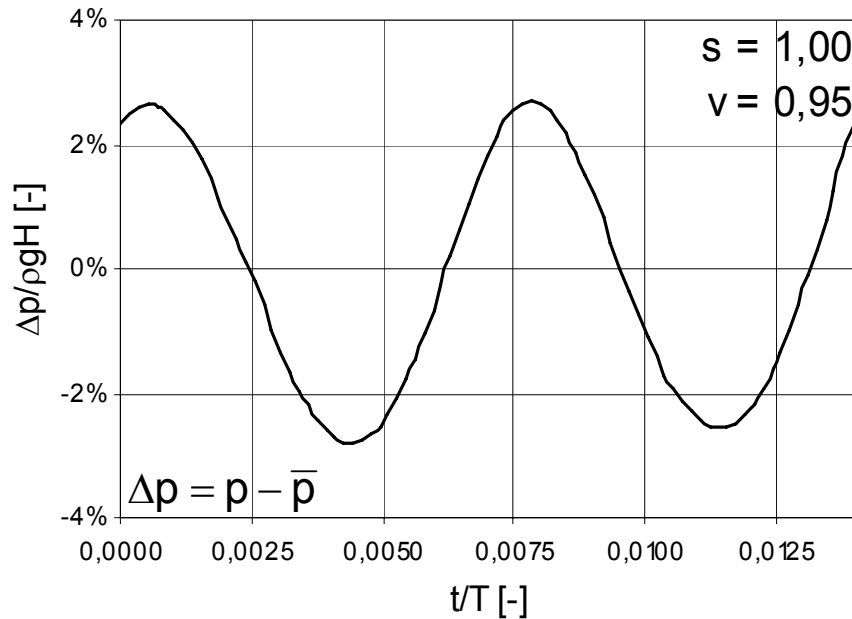


# Rated point results – Vortex shedding

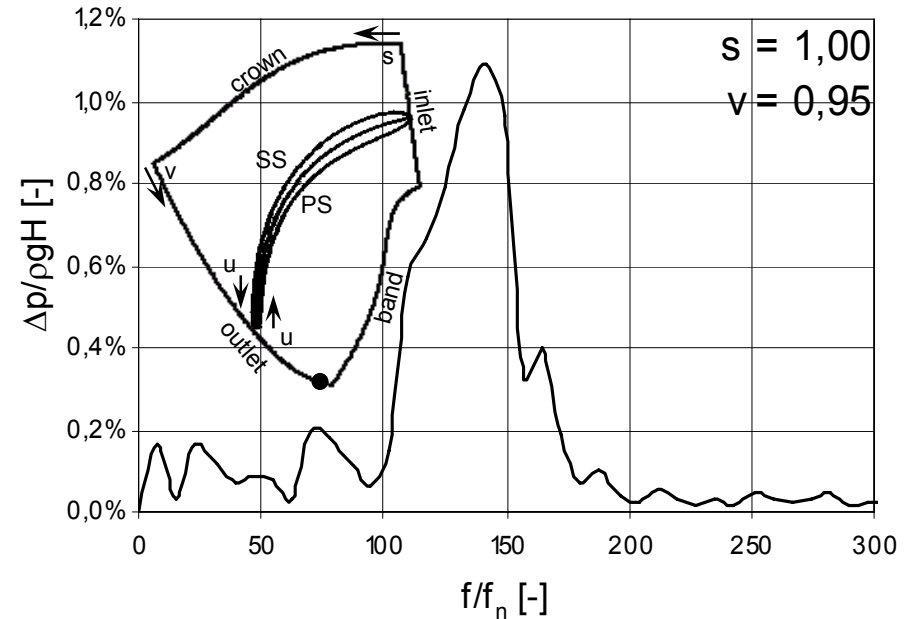


Vortex shedding at conformal view near to the band

# Vortex shedding – Time history

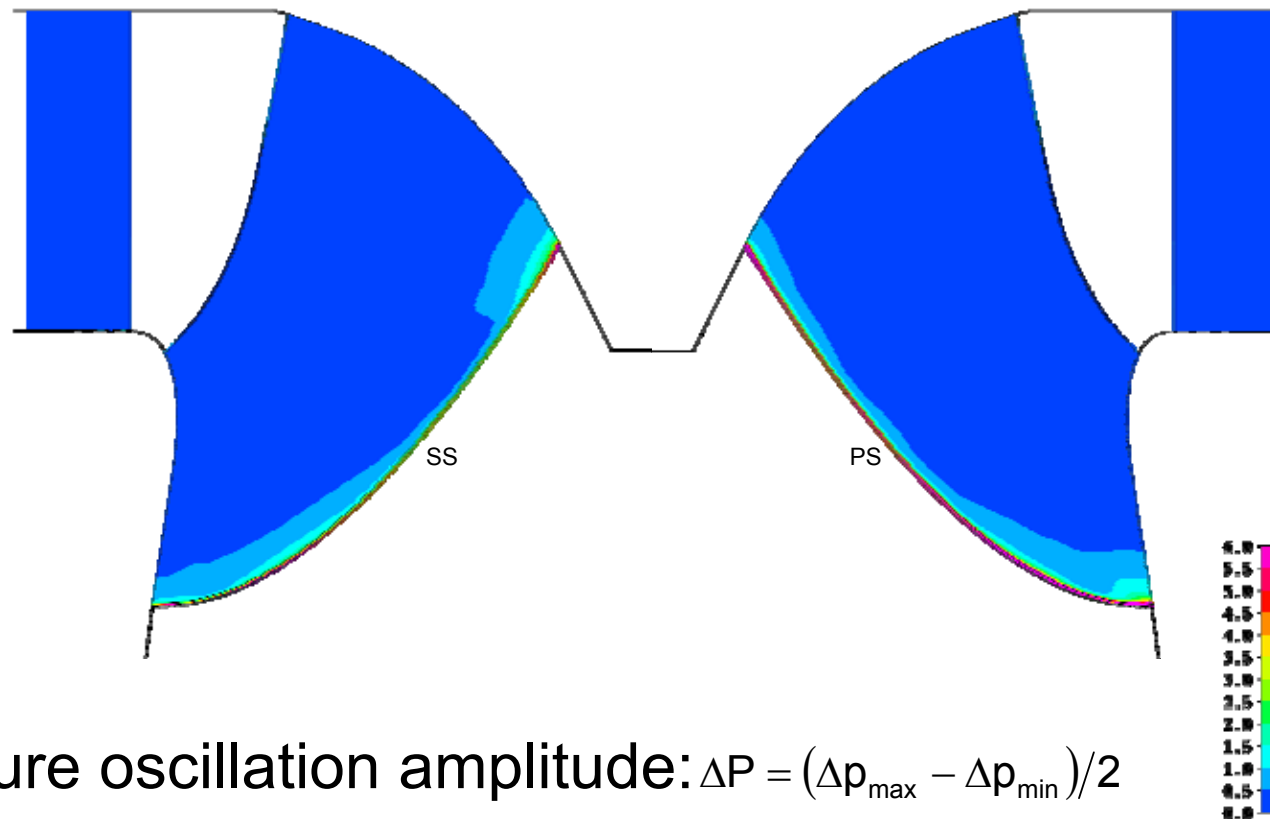


Time history at blade trailing edge near to the band



Fourier transform at blade trailing edge near to the band

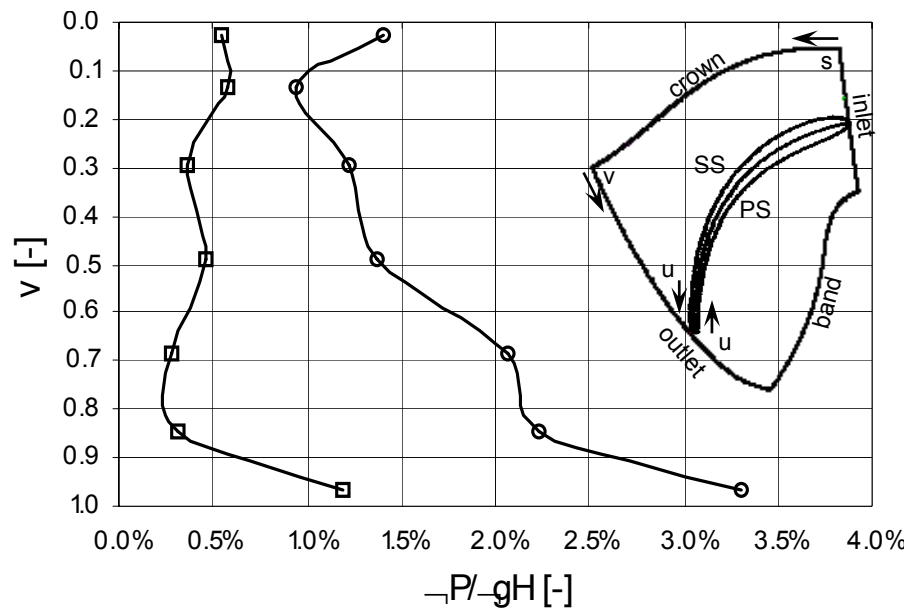
# Vortex shedding – Oscillation amplitude



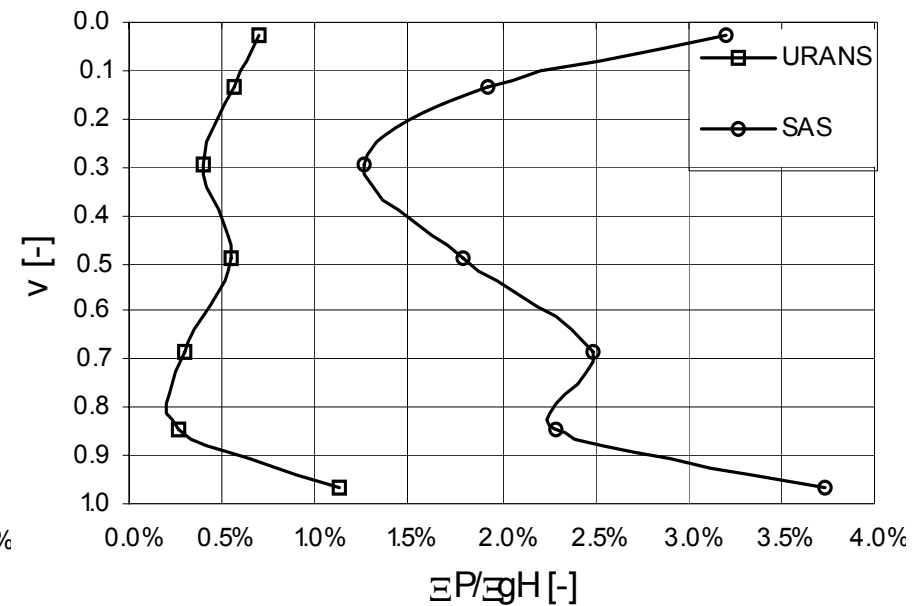
Pressure oscillation amplitude:  $\Delta P = (\Delta p_{\max} - \Delta p_{\min})/2$

Meridian view

# Vortex shedding – Oscillation amplitude

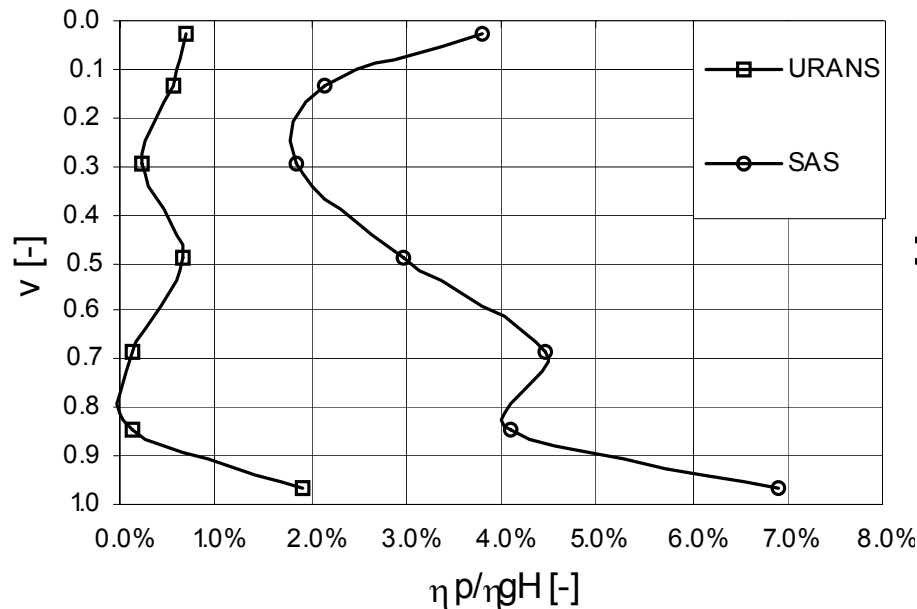


Turbulence models results at trailing edge at pressure side

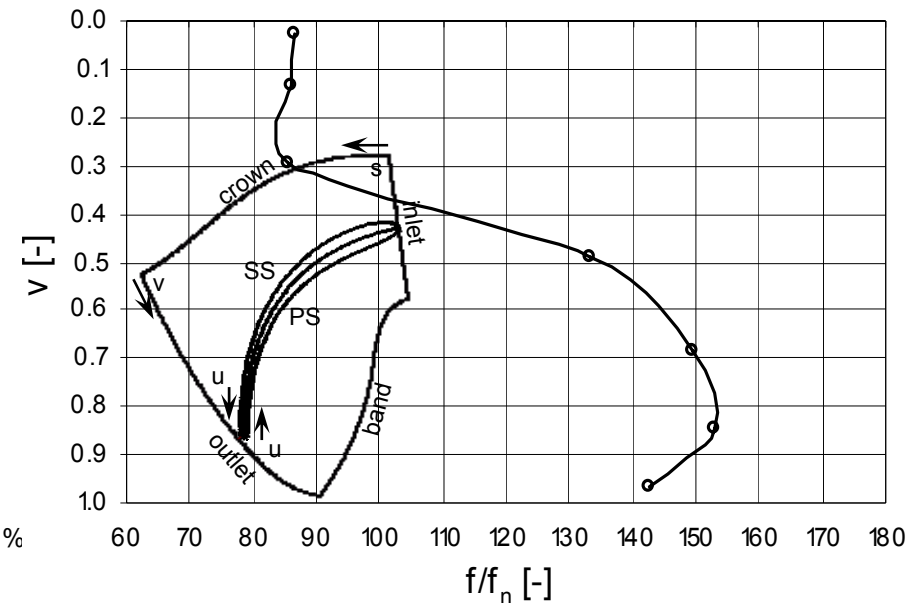


Turbulence models results at trailing edge at suction side

# Vortex shedding – Oscillation amplitude



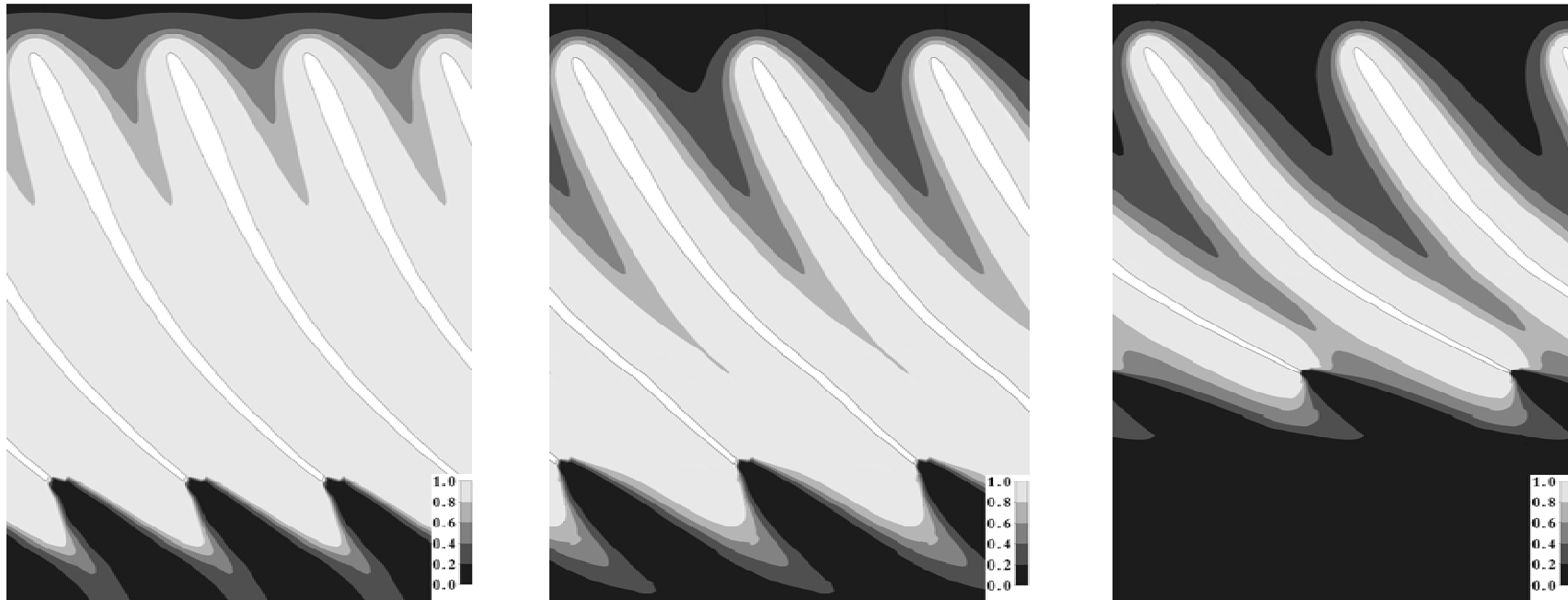
Turbulence models results at trailing edge: differential pressure between PS-SS



Turbulence models results at trailing edge: vortex shedding frequency



# Vortex shedding – Blending Function



Blending function for DES and SAS

Conformal planes  $v = 0,20$ ,  $v = 0,50$ ,  $v = 0,80$

# Vortex shedding – Comments

- Turbulence models:
  - Tested: URANS, SAS, DES
  - Best agreement with model test observed pattern: SAS and DES
- Pressure oscillation amplitude:
  - From 0,9%, in the vicinity of the crown
  - Up to 3,7%, in the vicinity of the band
- No synchronous frequency along the blade:
  - $\sim 150 \cdot f_n$  in the vicinity of the crown
  - $\sim 85 \cdot f_n$  in the vicinity of the band

# Vortex shedding – Comments

- Importance to the runner structural analysis:
  - Considerable amplitudes compared to RSI & DTI:
    - RSI: 0,3%-2,1% (excluding the leading edge region)
    - DTI: 0,6%-5,0% (excluding the leading edge region)
    - VSE: 0,9%-3,7%
  - The VSE pressure oscillation is applied at the runner structure weakest region:

Along the trailing edge, from the crown up to the band
  - High oscillating frequency:  
 $\sim 85 \cdot f_n - 150 \cdot f_n$

## Conclusions

- Ability to numerically predict pressure oscillations in Francis turbines
- Tight agreement between simulation and model test results
- No deviations between NS3D and CFX results
- Dynamic flow through the Francis turbine dominated by RSI, DTI and VSE

## Conclusions

- Importance of VSE for the pressure oscillations
- Need of adequate turbulence models such as SAS, DES and LES
- URANS not suited for part load and vortex shedding
- Accurate input available from the transient CFD results for the runner CSA
- Possibility to estimate the runner fatigue strength



## Next Steps

- Simulation of additional operating points in severe part load and overload conditions.
- Deeper investigation of the model constants in SAS and DES turbulence models.
- Evaluation of the fluid structure interaction.
- Assessment of the pressure oscillation effect on the structure strength and fatigue life.



# Thank you for your attention!