Technische Universität München
Fakultät für Informatik
Lehrstuhl für Effiziente Algorithmen
Prof. Dr. Harald Räcke
Chintan Shah

Summersemester 2012
Übungsblatt 8
June 22, 2012

Efficient Algorithms and Datastructures II

Aufgabe 1 (10 Punkte)

You have a system that consists of m slow machines and k fast machines. The fast machines can perform twice as much work per unit time as the slow machines. You are given a set of n jobs; job i takes time t_i to process on a slow machine and time $\frac{1}{2}t_i$ to process on a fast machine. You want to assign each job to a machine so as to minimize the makespan - the makespan is the maximum, over all machines, of the total processing time of jobs assigned to that machine.
Give a polynomial-time algorithm that produces as assignment of jobs to machines with a makespan that is at most three times the optimum.

Aufgabe 2 (10 Punkte)

Consider the following maximization version of the 3-Dimesnional Matching Problem. Given disjoint sets X, Y, Z and a set $T \subseteq X \times Y \times Z$ of ordered triples, a subset $M \subseteq T$ is a 3-dimensional matching if each element of $X \cup Y \cup Z$ is contained in at most one of these triples. The Maximum 3-Dimensional Matching Problem is to find a 3-dimensional matching M of maximum cardinality.
Give a polynomial-time algorithm that finds a 3-dimensional matching of size at least $\frac{1}{3}$ times the maximum possible size.

Aufgabe 3 (10 Punkte)

Show that for any input to the problem of minimizing the makespan on identical parallel machines for which the processing requirement of each job is more than $\frac{1}{3}$rd the optimal makespan, the longest processing time rule computes an optimal schedule.